



Centre of Mathematics (CMAT), University of Minho

Spatio-temporal variability of the distribution and abundance of small pelagic fish off the Portuguese continental coast and relationship with environmental drivers

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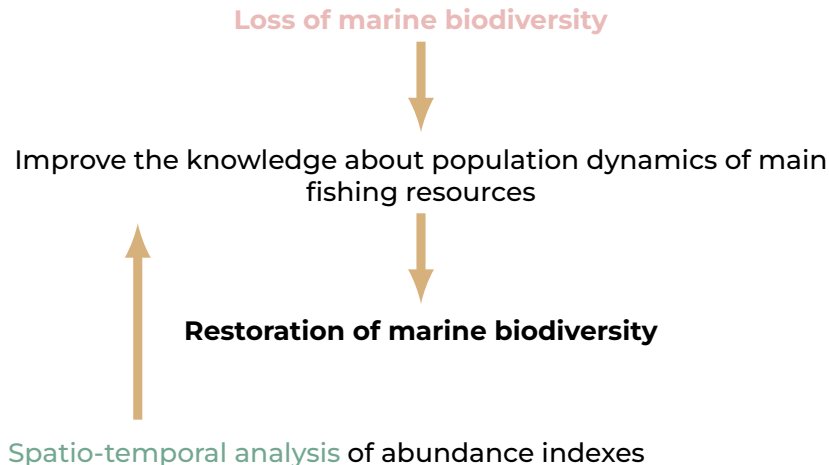
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Susana Garrido, IPMA

Scope of the work



Motivating data



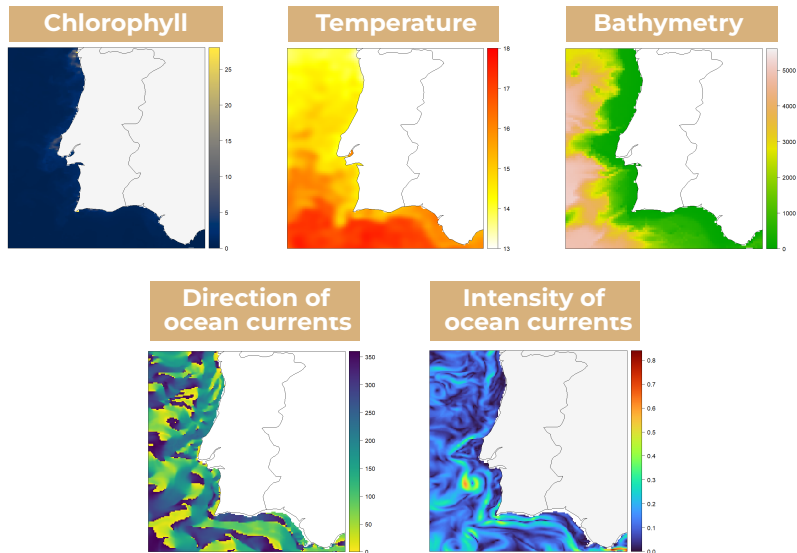
PELAGO surveys

Estimate the abundance of sardine inhabiting the Portuguese shelf.

Database

Time:	20 annual surveys from 2000 to 2020, except 2012.
Study region:	Portuguese continental coast and Gulf of Cadiz.
Interest:	Biomass index (NASC, $n^2 \text{ nm}^{-2}$).
Geographic information:	Latitude and longitude.
Additional information:	Sectors and geographical areas.

Environmental data



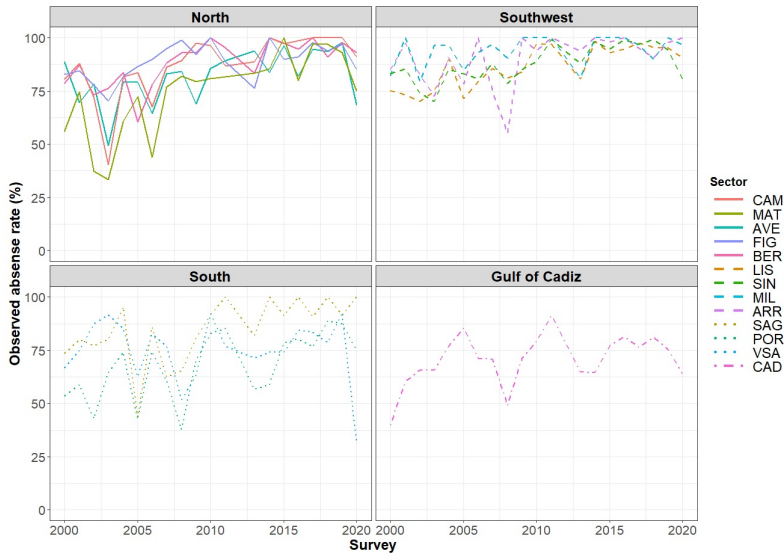
Species Distribution Data often implies residual **spatial autocorrelation**

- **Non-consideration** of important environmental conditions.
- **Intrinsic factors:** competition, dispersal, aggregation, etc.

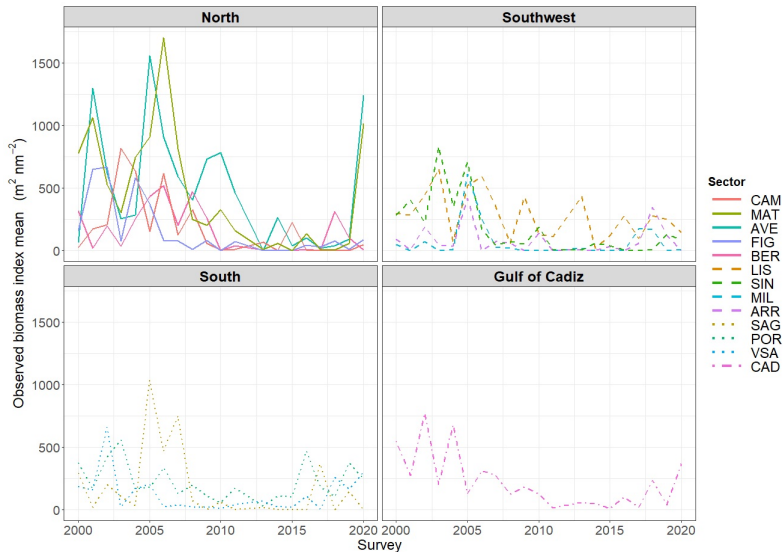


Geostatistics

Problem and Objective



Problem and Objective



Problem and Objective

Main aims

- Estimate the **spatio-temporal distribution** of sardine in western and southern Iberian waters.
- Understand sardine dynamics over time and space.
- Identify the **main drivers** of sardine spatial dynamics.

To consider:

- Complex spatio-temporal dynamics.
- Excess of zeros.
- Difference between occurrence process and biomass process under occurrence.
- Relationship between response and **environmental conditions with a time lag**.

Two-part model

Hierarchical model

Series of levels linked by probability functions.

Y_{st} - **Biomass process** at location s and time t

Z_{st} - **Occurrence sub-process**

Distribution of biomass index

$$\begin{aligned} [Y_{st}] &= [Z_{st}] [Y_{st} | (Z_{st} = 1)] \\ &= \begin{cases} 1 - \pi_{st}, & y_{st} = 0 \\ \pi_{st} [Y_{st} | (Z_{st} = 1)], & y_{st} > 0 \end{cases} \end{aligned}$$

such that:

$$\begin{aligned} Z_{st} &\sim \text{Bernoulli}(\pi_{st}) \\ Y_{st} | (Z_{st} = 1) &\sim \text{Gamma}(a_{st}, b_{st}) \end{aligned}$$

Two-part model

Two-part model can be defined by:

$$\log(\mu_{sti}) = \alpha + \sum_{j=1}^p \mathbf{f}(K(X_{jsti}, c, l)) + \gamma_t + W_{st}$$

$$\text{logit}(\pi_{sti}) = \alpha' + \sum_{j=1}^{p'} \mathbf{f}'(K(X'_{jsti}, c, l)) + \gamma'_t + k W_{st}$$

time lag $c + l$ in days from i^{th} day of the survey in year t ,

smoother function \mathbf{f} of the j^{th} covariate X_{jsti} ,

spatio-temporal structure W_{st} ,

unstructured temporal effects γ_t and γ'_t .

$$W_{st} = \delta W_{s(t-1)} + \xi_{st}$$

- 1 $|\delta| < 1$
- 2 ξ_{st} is a zero-mean GF with spatio-temporal covariance:

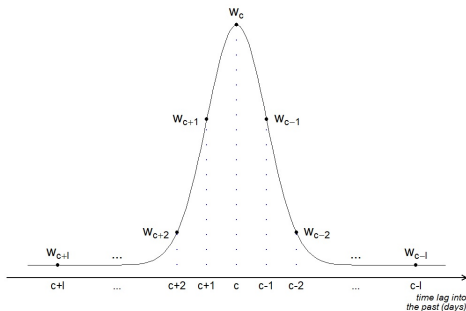
$$\text{Cov}(\xi_{st}, \xi_{uj}) = \begin{cases} 0 & \text{if } t \neq j \\ \text{Cov}(\xi_s, \xi_u) & \text{if } t = j \end{cases}$$

such that $\text{Cov}(\xi_s, \xi_u)$ is given by **Matérn spatial covariance** with partial variance σ^2 and range ϕ .

Kernel application $K(., ., .)$

$$K(X_{jst}, c, l) = \sum_{q=-l}^l w_{c-q} X_{jst(i-(c-q))}$$

- $w_{c-q} = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{q^2}{2h^2}\right\}$
- $X_{jst(i-(c-q))}$ - j^{th} covariate observed in day $i - (c - q)$ of year t
- On the i^{th} day, the maximum effect of X_j occurs for lag c

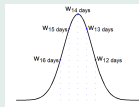


Examples of Kernel application

Presence/absence modelling:

$$\text{logit}(\pi_{sti}) = \alpha_1 + \sum_{j=1}^{p'} f(K(X'_{jsti}, c, l)) + \gamma'_t + kW_{st}$$

- 1 If the biomass **is only affected by chlorophyll on the same day**, then
 $K(CHL_{sti}, 0, 0) = CHL_{sti}$
- 2 If the biomass **is affected by chlorophyll 14 days ago**, then
 $K(CHL_{sti}, 14, 0) = CHL_{st(i-14)}$
- 3 If the biomass **is affected by chlorophyll 14 days earlier and 2 days before and after**, then
 $K(CHL_{sti}, 14, 2) = w_{16}CHL_{st(i-16)} + w_{15}CHL_{st(i-15)} + w_{14}CHL_{st(i-14)} + w_{13}CHL_{st(i-13)} + w_{12}CHL_{st(i-12)}$



Advantages

- It allows to **incorporate prior information**.
- **Information and uncertainty** about all the unknown can be better (and easily) **expressed in terms of probability distributions**.
- It might more **easily handle with inference and prediction** (Banerjee, Carlin, and Gelfand 2004).

Inference method

INLA approach was used to approximating the posterior marginals of the latent GF (Rue, Martino, and Chopin 2009).

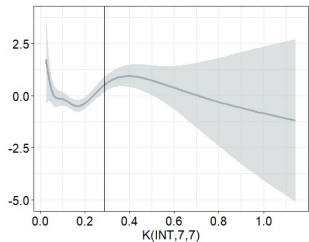
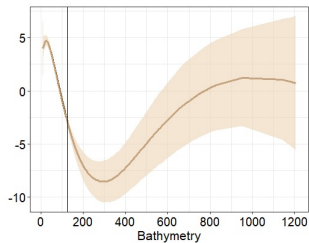
<https://www.r-inla.org/>

Some highlights

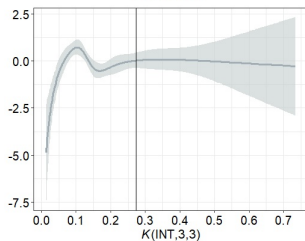
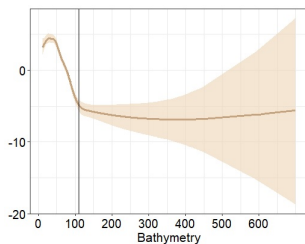
- Various **combinations of c and l** were tested.
- Data from the west and south Iberian coasts are **studied separately**.
- Spatial predictions over the entire study region were obtained **for a "representative day"** of each survey for the total 21 years.

Results: Environmental effects for the presence

Effects on west coast



Effects on south coast

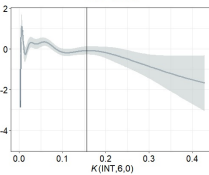
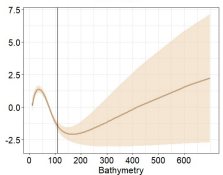
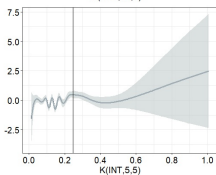
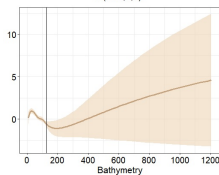
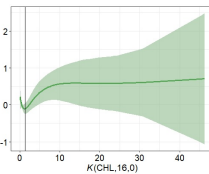
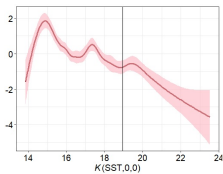
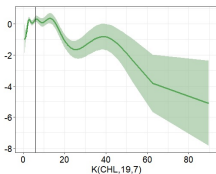
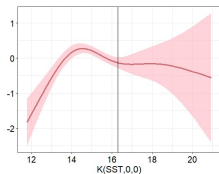


*vertical line - quantile 80%

Results: Environmental effects for the biomass

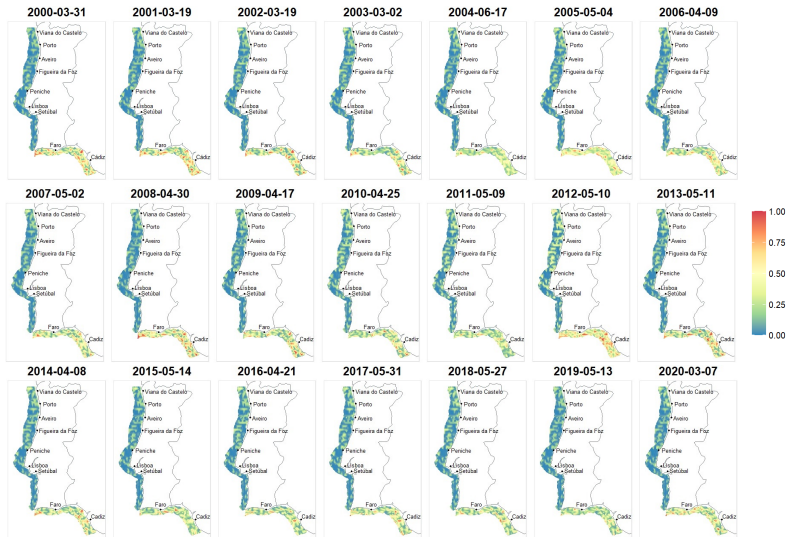
Effects on west coast

Effects on south coast

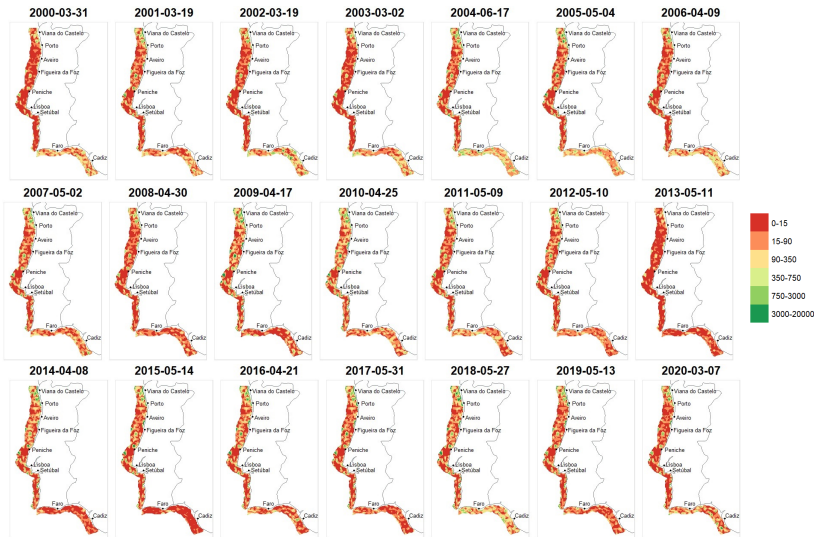


*vertical line - quantile 80%

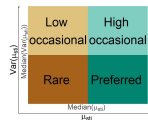
Results: Predicted occurrence



Results: Predicted biomass

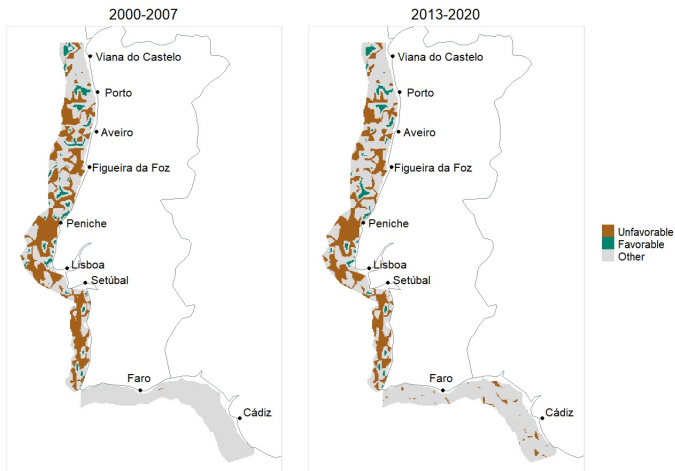


Results: Occupancy areas



Results: Favourable and unfavourable zones

Persistent rare (unfavourable) and preferred (favourable) zones



On going work

- Apply this methodology to the **anchovy data**.

Future work

- Model the spatio-temporal distribution of sardine from data obtained from commercial fisheries, taking into account **preferential sampling**.
- **Joint modelling** fishery-dependent and fishery-independent data.

Thank you for your attention!

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