

**Numerical modeling of the slow-growing,  
motile harmful alga *Gymnodinium catenatum*  
in Inokushi Bay, a small inlet in southern Japan**

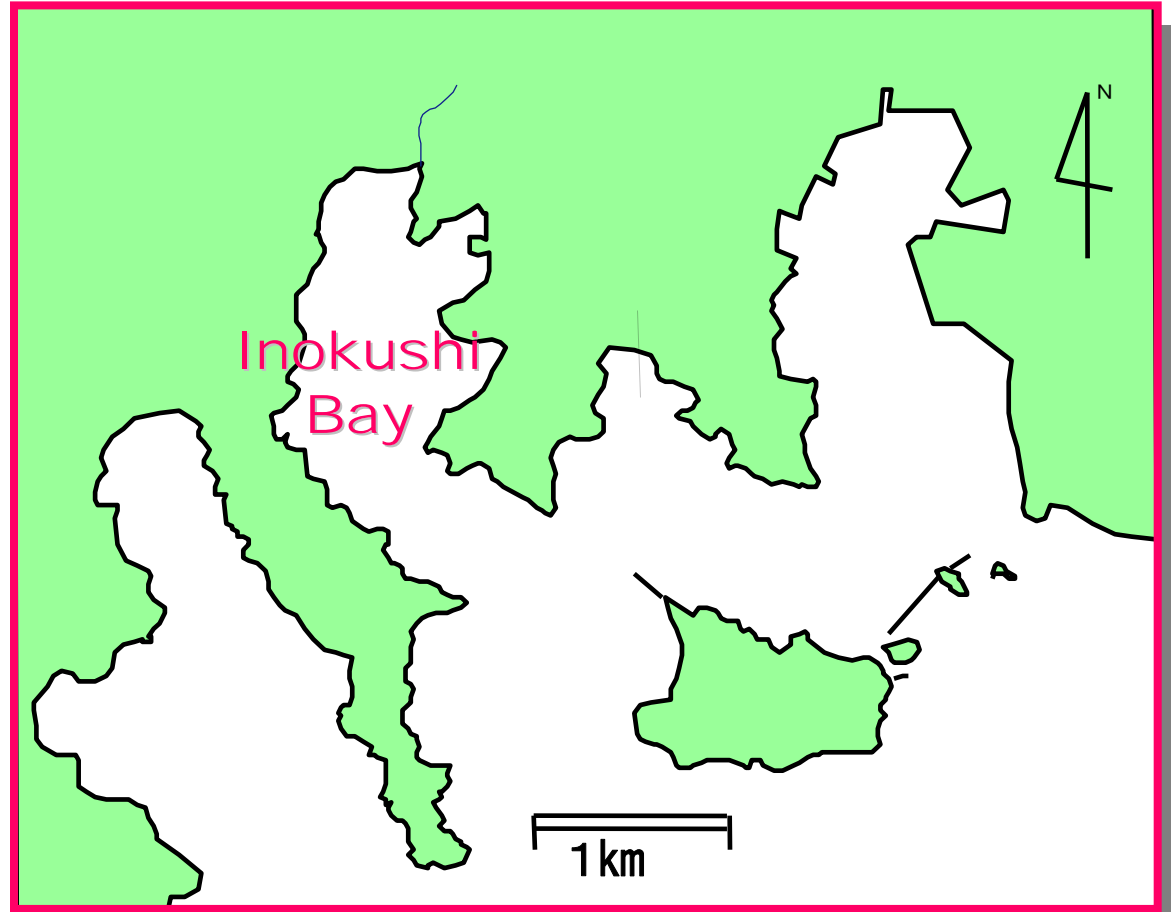


*G. catenatum*

**Tamiji YAMAMOTO and Ryoko SAKAI**

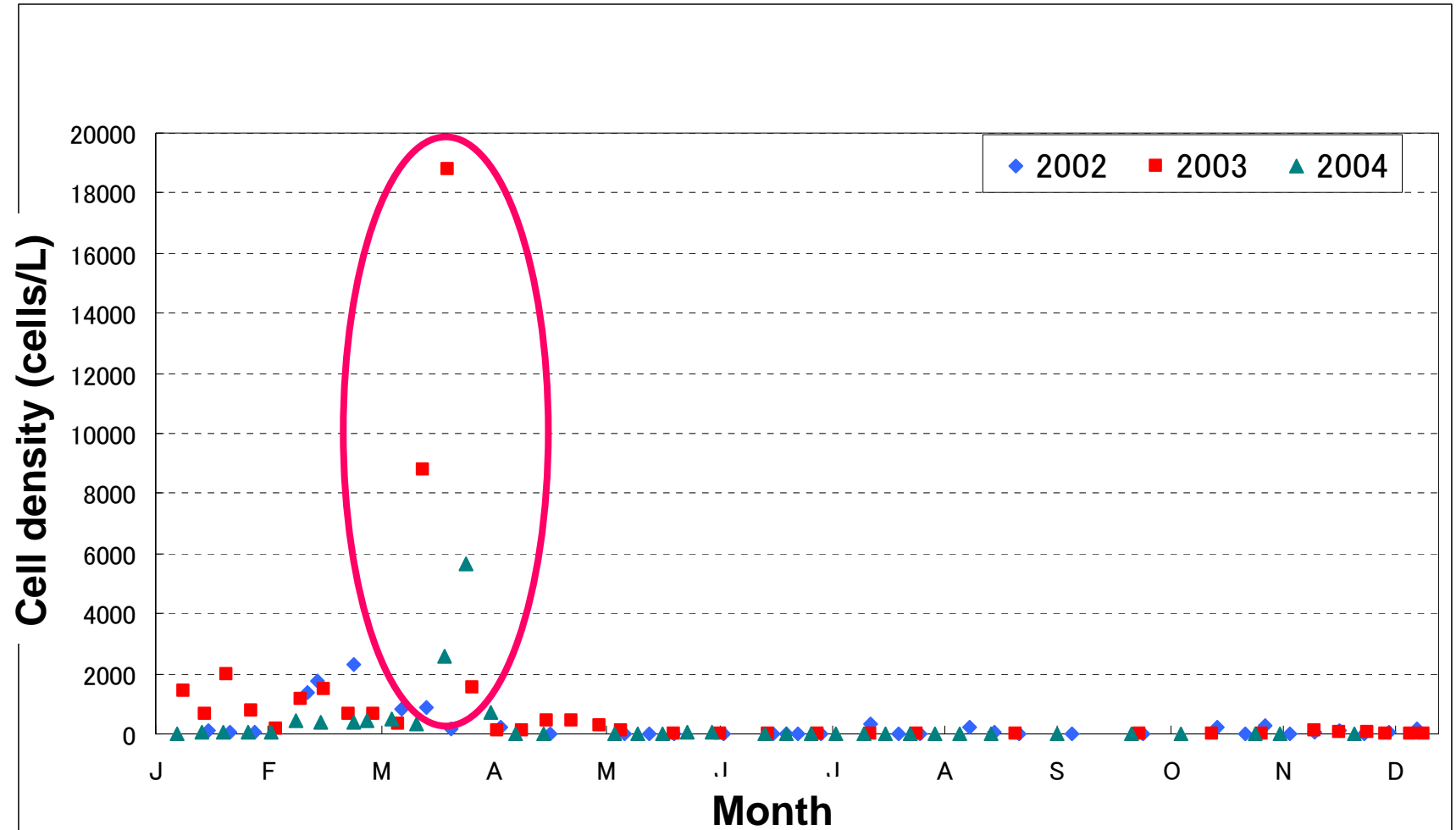
**Graduate School of Biosphere Science,  
Hiroshima University, Japan**

# Inokushi Bay, Japan



**Toxification of noble scallops and other shellfish**

# Cell density of *G. catenatum* in Inokushi Bay, Japan



# Purpose

$\mu_{\max}=0.31/\text{day}$  (25°C, 30 psu)

(Yamaguchi, pers. comm.)

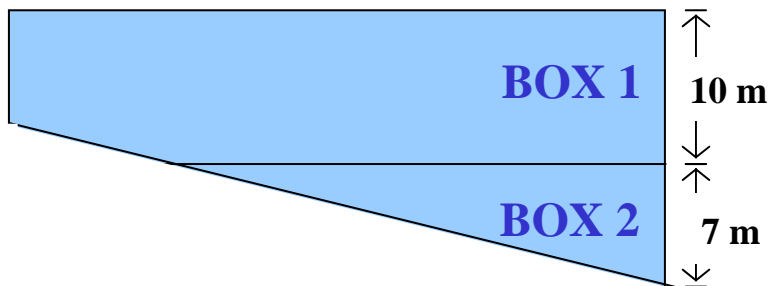
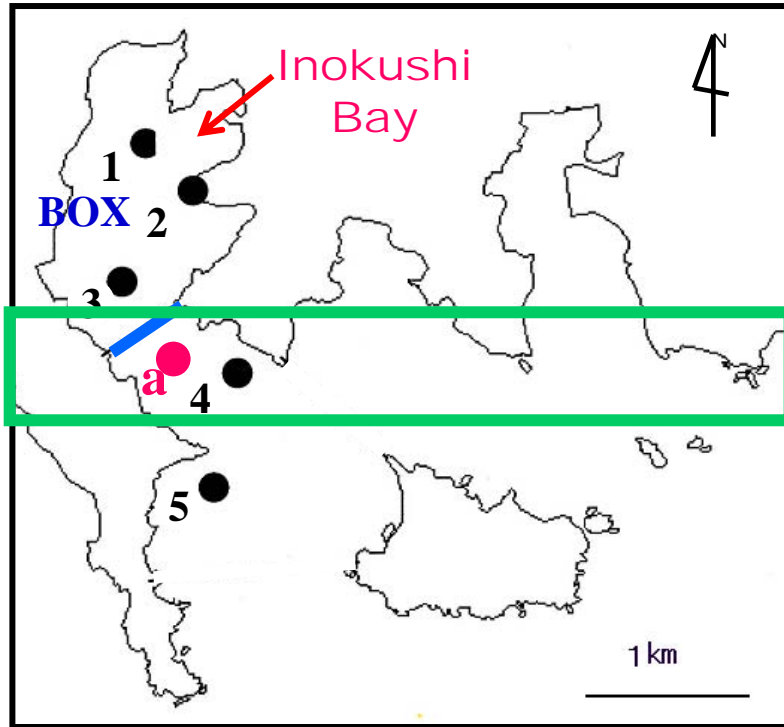
**Question:**

**Why is this species able to form blooms in Inokushi Bay with such a low growth rate?**

**To understand the bloom forming mechanisms of *G. catenatum* in Inokushi Bay using a numerical model**

# Methods

## Arrangement of boxes



<Observation> 25 Nov 2003-12 Apr 2004

<Parameters>

<Stations>

Temperature	● St.1-5
Salinity	
Nutrients	● St.a
Cell density	
Current velocity	

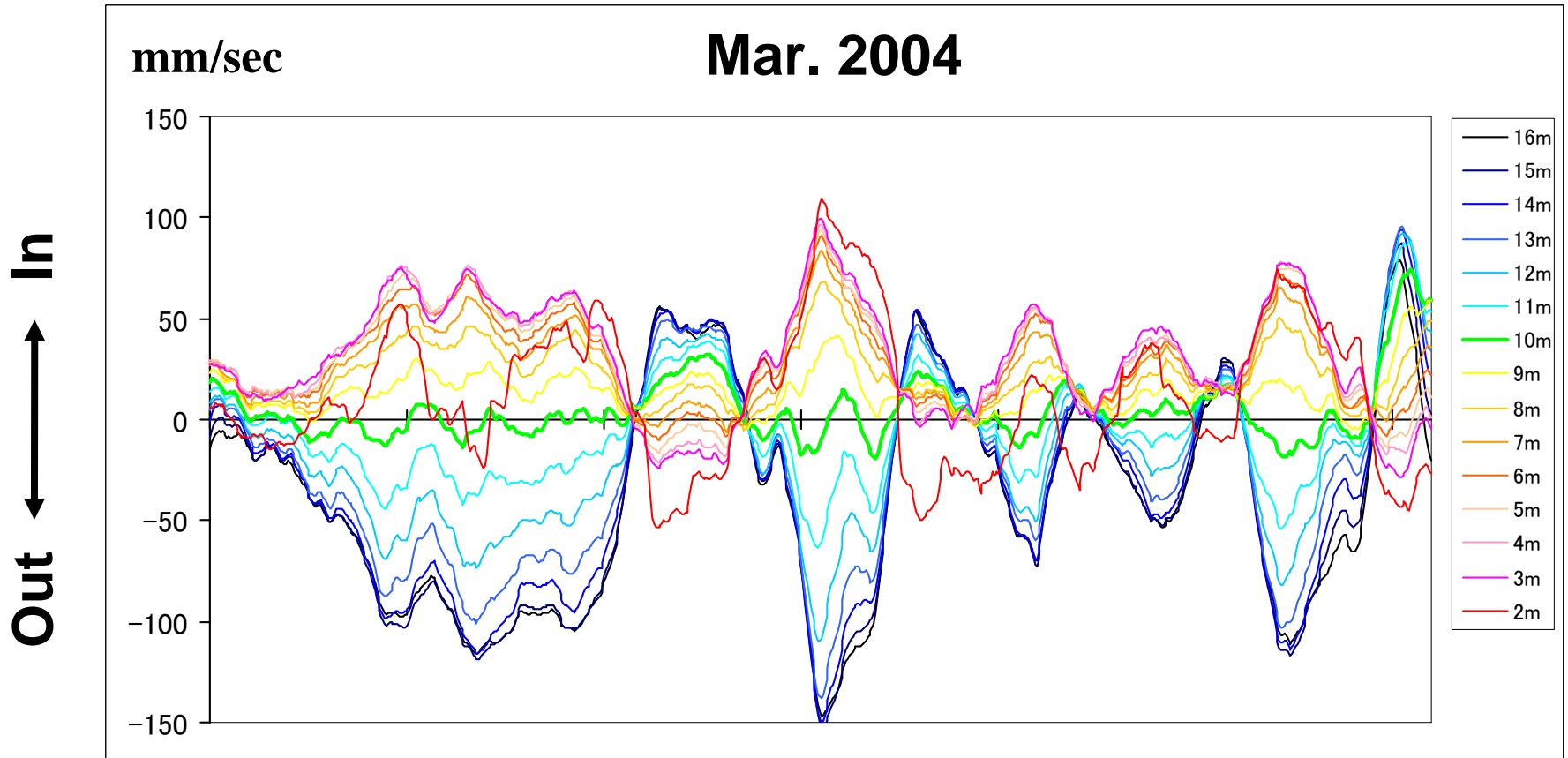
## BOX sizes

	BOX 1 (upper)	BOX 2 (lower)
Surface area	1.94 km <sup>2</sup>	1.36 km <sup>2</sup>
Depth	0-10 m	10-17 m
Area of cross section	5,600 m <sup>2</sup>	3,920 m <sup>2</sup>

# Current velocity

● St.a, Doppler Current Meter  
Running mean of 25 hrs.

Abo (pers. comm.)



**When the water comes in to the upper layer (0-10 m),  
the water of lower layer (10 m-B) is pushed out of the bay.**



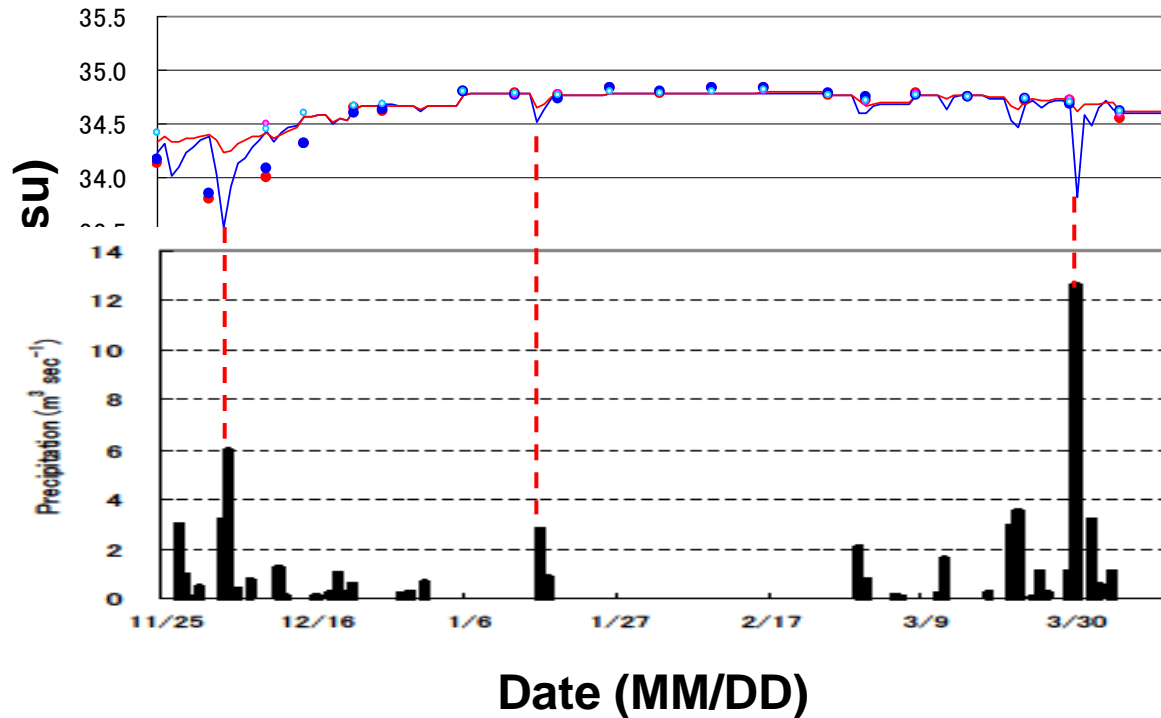
# Diffusion coefficients

$$V_1 \frac{S_{1a} - S_1}{dt} = Kh_1 \times \frac{S_{1_{out}} - S_1}{X_1} \times Ah_1 + K_V \times \frac{S_2 - S_1}{Z} \times Av - Vh_{1_{adv}} \times Ah_1 \times Sh_1 - V_{V_{adv}} \times Av \times Sv - (P - E)S_1$$

$$V_2 \frac{S_{2a} - S_2}{dt} = Kh_2 \times \frac{S_{2_{out}} - S_2}{X_2} \times Ah_2 + K_V \times \frac{S_1 - S_2}{Z} \times Av - Vh_{2_{adv}} \times Ah_2 \times Sh_2 + V_{V_{adv}} \times Av \times Sv$$

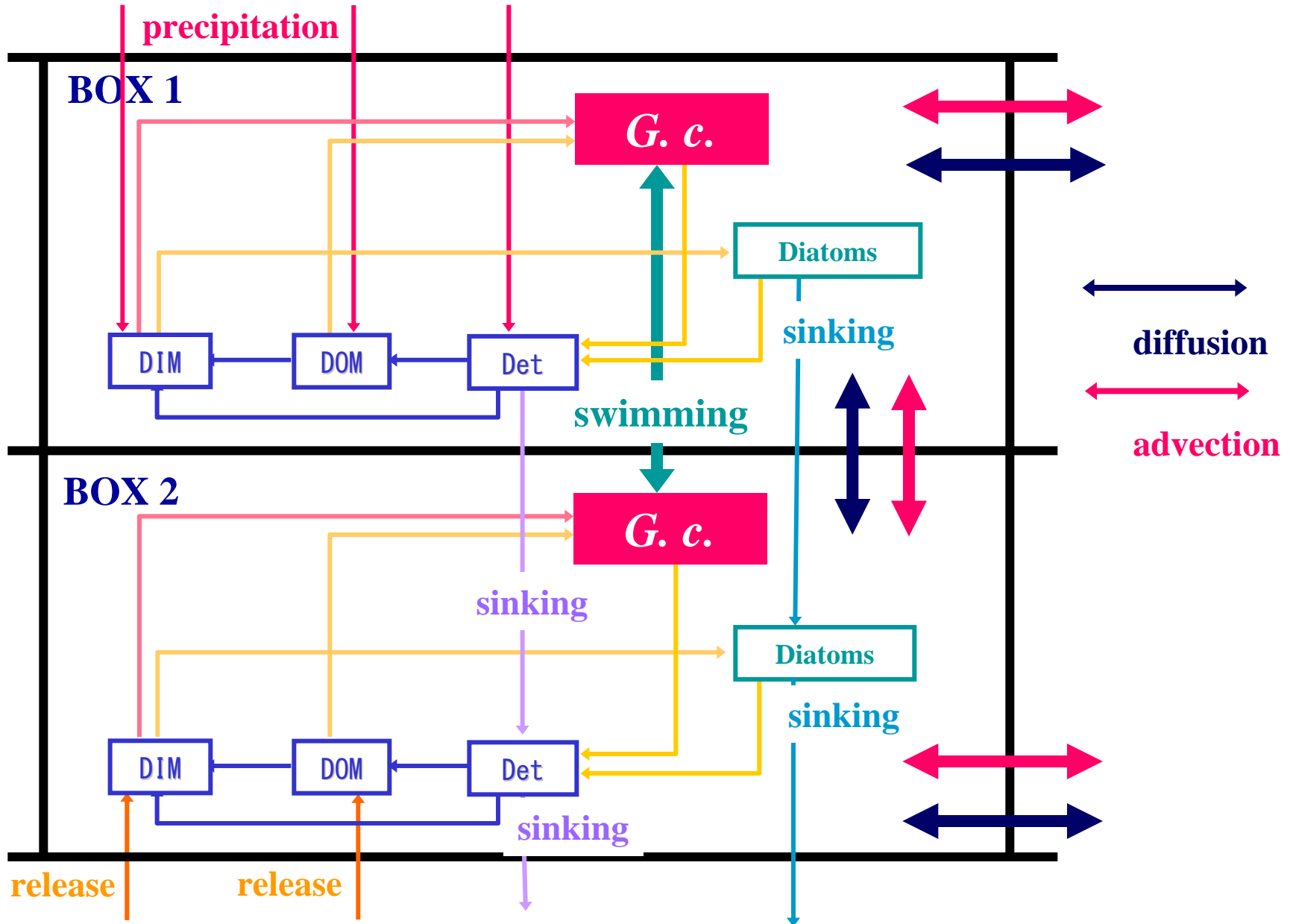
Horizontal dif. coef.  $1.0 \sim 1.0 \times 10^3 \text{ m}^2 \text{ sec}^{-1}$

Vertical dif. coef.  $1.0 \times 10^{-5} \sim 1.0 \times 10^{-3} \text{ m}^2 \text{ sec}^{-1}$





# Framework of ecosystem model



# Mass balance (P, upper layer)

## Time change in DIP

$$V_{1U} \frac{dDIP_{1U}}{dt} = -V_{1U} (\rho_{Ud} PHYd(P)_{1U} + \rho_{Ugdip} PHYg(P)_{1U} - C_1 PP(P)_{1U} - D_1 DOP_{1U}) \\ - V_{adv} \times DIP_{1U} + V_{adv} \times DIP_{1L} - AH_{1U} \frac{KH_{1U}}{X_{1U}} (DIP_{1U} - DIP_{OU}) - AV_1 \frac{KV_1}{Z_1} (DIP_{1U} - DIP_{1L})$$

## Time change in DOP

$$V_{1U} \frac{dDOP_{1U}}{dt} = -V_{1U} (\rho_{Ugdop} PHYg(P)_{1U} - C_2 PP(P)_{1U} + D_1 DOP_{1U}) \\ - V_{adv} DOP_{1U} + V_{adv} \times DOP_{1L} - AH_{1U} \frac{KH_{1U}}{X_{1U}} (DOP_{1U} - DOP_{OU}) - AV_1 \frac{KV_1}{Z_1} (DOP_{1U} - DOP_{1L})$$

## Time change in Det-P

$$V_{1U} \frac{dDetP_{1U}}{dt} = +V_{1U} (A_{3Ud} PHYd(P)_{1U} + A_{3Ug} PHYg(P)_{1U} - C_1 DetP(P)_{1U} - C_2 DetP(P)_{1U}) \\ - AV_1 Sink_{PP} DetP(P)_{1U} - AH_{1U} \frac{KH_{1U}}{X_{1U}} (DetP_{1U} - DetP_{OU}) - AV_1 \frac{KV_1}{Z_1} (DetP_{1U} - DetP_{1L}) \\ - V_{adv} \times DetP_{1U} + V_{adv} \times DetP_{1L}$$

## Time change in PHYg (*G. catenatum*)

$$V_{1U} \frac{dPHYg_U}{dt} = V_{1U} (\mu_{Ugdip} PHYg_U + \mu_{Ugdop} PHYg_U - A_{Ug} PHYg_U) - AV_1 Swim_{Pg} PHYg_U \\ - V_{adv} \times PHYg_U + V_{adv} \times PHYg_L - AH_{1U} \frac{KH_{1U}}{X_{1U}} (PHYg_U - PHYg_{OU}) - AV_1 \frac{KV_1}{Z_1} (PHYg_U - PHYg_L)$$

## Time change in PHYd (Diatoms)

$$V_{1U} \frac{dPHYd_{1U}}{dt} = V_{1U} (\mu_U PHYd_{1U} - A_{3U} PHYd_{1U}) - AV_1 Sink_{Pd} PHYd_{1U} \\ - V_{adv} \times PHYd_{1U} + V_{adv} \times PHYd_{1L} - AH_{1U} \frac{KH_{1U}}{X_{1U}} (PHYd_{1U} - PHYd_{OU}) - AV_1 \frac{KV_1}{Z_1} (PHYd_{1U} - PHYd_{1L})$$

# Biological processes

## □Temp. & Sal.

### *G. catenatum*

$$\mu_{st} = 1.2842 - 0.2767 \times T + 0.016 \times T^2 - 0.0004 \times S^2 + 0.0023 \times T \times S - 0.0003 \times T^3 - 0.00004 \times T^2 \times S$$

(Yamaguchi, pers. comm.)

### Diatom (*S. costatum*)

$$\mu_t = -0.004 \times T^2 + 0.165 \times T - 0.766$$

$$\mu_s = -0.003 \times S^2 + 0.132 \times S - 0.226$$

(Tsuruta et al., 1985)

## □Light

### *G. catenatum*

$$\mu_i = \mu'_{\max} \times \frac{I - 10}{I - 3.2}$$

(Yamamoto et al., 2002)

### Diatom (*S. costatum*)

$$\mu_i = \mu'_{\max} \times \frac{I - 5.43}{(60.8 - 5.43) + (I - 5.43)}$$

(Langdon, 1987)

## □Nutrient uptake *G. catenatum* Diatom (*S. costatum*)

$$\rho = \rho_{\max} \times \frac{S}{S + K_S} \quad (\text{Dugdale, 1967})$$

$$\mu_e = \mu'_{\max} (1 - Q_{\min} / Q_e) \quad (\text{Droop, 1973})$$

$$Q_{\max} = \left( \frac{\mu'_{\max}}{\mu'_{\max} - \mu_{\max}} \right) \times Q_{\min}$$

(Morel, 1987)

$$\rho_{\max} = \rho_{\max}^{hi} - \frac{(\rho_{\max}^{hi} - \rho_{\max}^{lo}) \times (Q - Q_{\min})}{(Q_{\max} - Q_{\min})}$$

$$\rho_{\max}^{lo} = \mu'_{\max} \times (Q_{\max} - Q_{\min}) \quad (\text{Grover, 1991})$$

# Biological processes (cont'd)

## □ Growth rate

*G. catenatum*

$$\mu = \mu'_{\max} \times \min(f(e), f(i)) \times \frac{\mu_{st}}{\mu'_{\max ST}}$$

Diatom (*S. costatum*)

$$\mu = \mu_e \times \frac{\mu_t}{\mu_{\max t}} \times \frac{\mu_s}{\mu_{\max S}} \times \frac{\mu_i}{\mu_{\max i}}$$

## □ Mortality rate

$$A_3 = M_{po} \exp(k_{MP} T)$$

## □ Decomposition rate of PP to DIP and DOP

$$C_1 = V_{PI} \exp(k_{VPI} T)$$
$$C_2 = V_{PO} \exp(k_{VPO} T)$$

## □ Decomposition rate of DOP to DIP

$$D_1 = V_{DIP} \exp(k_{VDI} T)$$

# Parameters used in this model

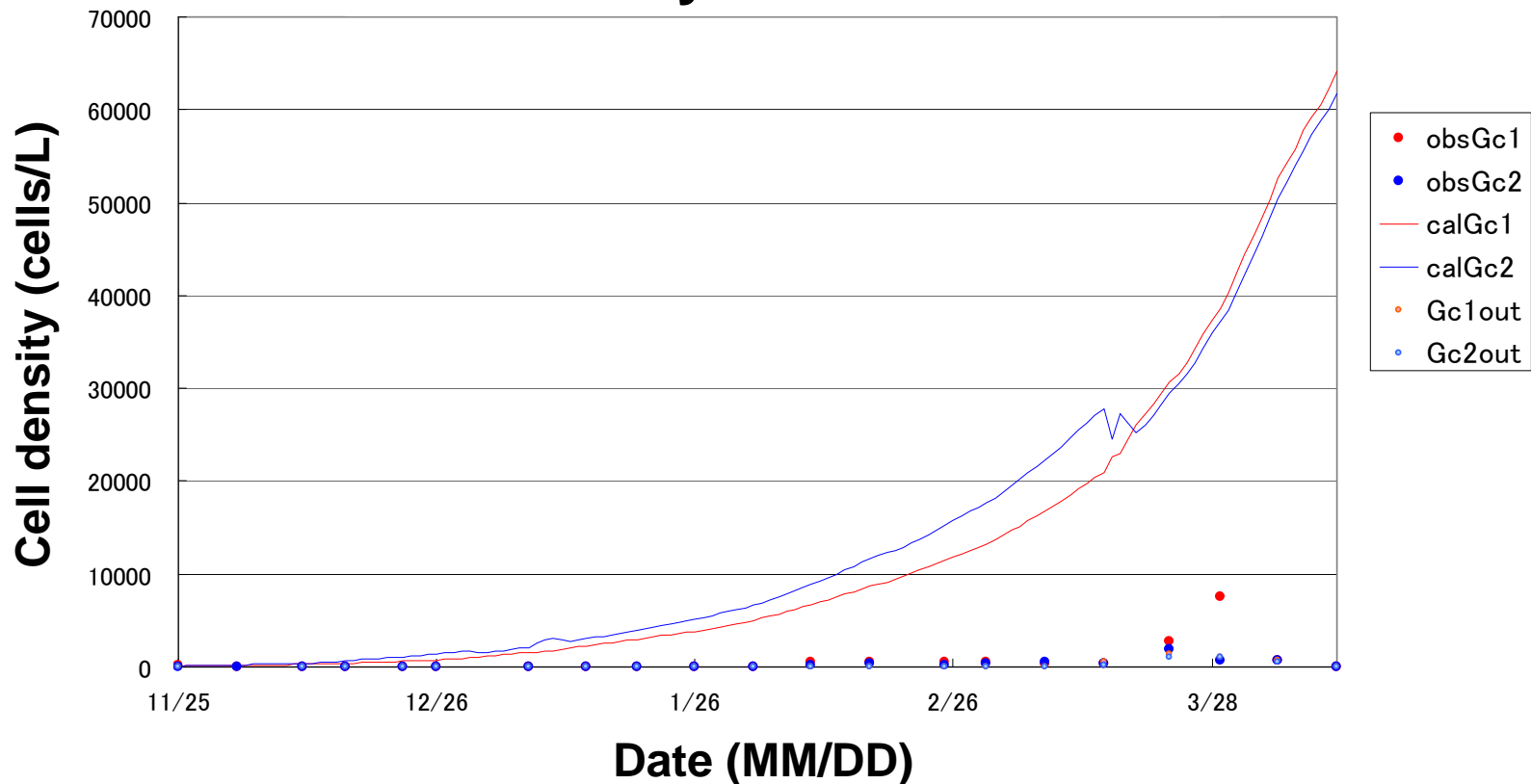
symbols	values	unit	references
<b><i>Gymnodinium catenatum</i></b>			
$\mu_{\max}$	0.31	d <sup>-1</sup>	Kann (2000)
$\mu'_{\max(P)}$	0.53	d <sup>-1</sup>	yamaguchi
$K_s$ (DIP)	3.4	$\mu$ M	Kataoka (2001)
$K_s$ (DOP)	7.61	$\mu$ M	Oh(2002)
$\rho_{\max}^{hi}$ (DIP)	1.42	pmol cell <sup>-1</sup> h <sup>-1</sup>	Kataoka (2001)
$\rho_{\max}^{hi}$ (DOP)	13.38	pmol cell <sup>-1</sup> h <sup>-1</sup>	Oh(2002)
$\rho_{\max}^{lo}$ (P)	0.15	pmol cell <sup>-1</sup> h <sup>-1</sup>	*1
$Q_0$ (P)	1.44	pmol cell <sup>-1</sup>	yamaguchi
$Q_{\max}$ (P)	3.43	pmol cell <sup>-1</sup>	*2
$W$ (dinoflagellate)	14.88	m day <sup>-1</sup>	Anderson and Stolzenbach(1985)
<b><i>Skeletonema costatum</i></b>			
$\mu_{\max}$	0.96	d <sup>-1</sup>	yamaguchi
$\mu'_{\max(P)}$	1.25	d <sup>-1</sup>	tarutani and yamamoto(1994)
$K_s$ (DIP)	0.68	$\mu$ M	tarutani and yamamoto(1994)
$\rho_{\max}^{hi}$ (DIP)	0.038	pmol cell <sup>-1</sup> h <sup>-1</sup>	tarutani and yamamoto(1994)
$\rho_{\max}^{lo}$ (P)	0.02	pmol cell <sup>-1</sup> h <sup>-1</sup>	*1
$Q_0$ (P)	0.004	pmol cell <sup>-1</sup>	tarutani and yamamoto(1994)
$Q_{\max}$ (P)	0.02	pmol cell <sup>-1</sup>	*2
Sinking	0.7	m day <sup>-1</sup>	Smayda(1970)

\*1: calculate with  $\mu'_{\max} = \rho_{\max}^{lo} / (Q_{\max} - Q_0)$

\*2: calculate with  $Q_{\max} = \mu'_{\max} \times Q_{\min} / (\mu'_{\max} - \mu_{\max})$

# Results – primary calculation: with no physical processes

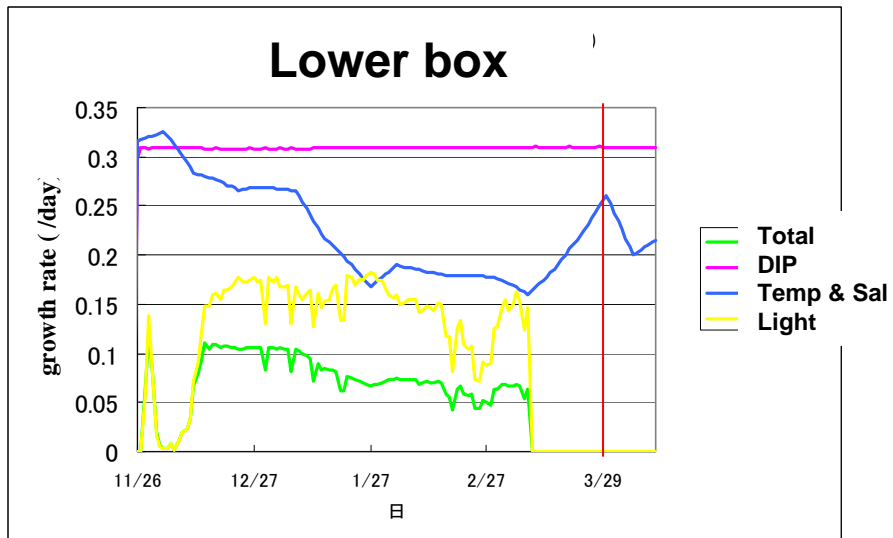
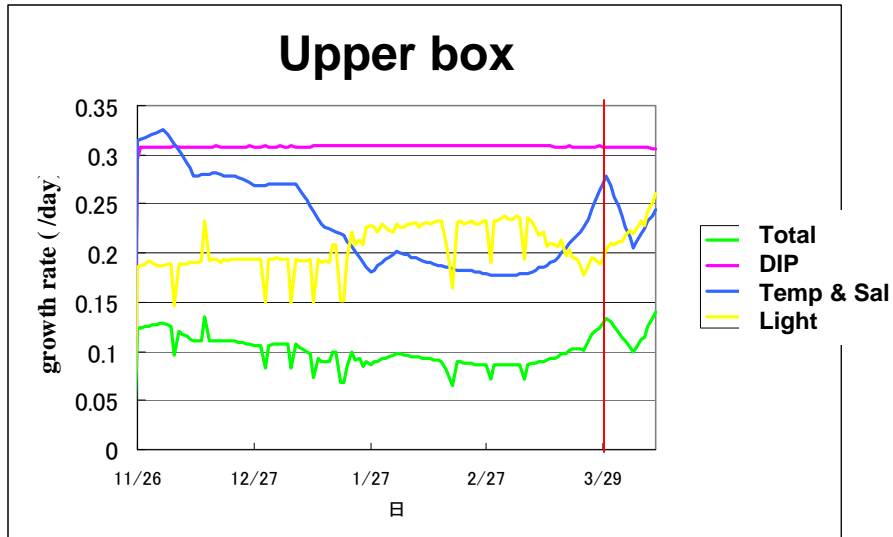
## Cell density of *G. catenatum*



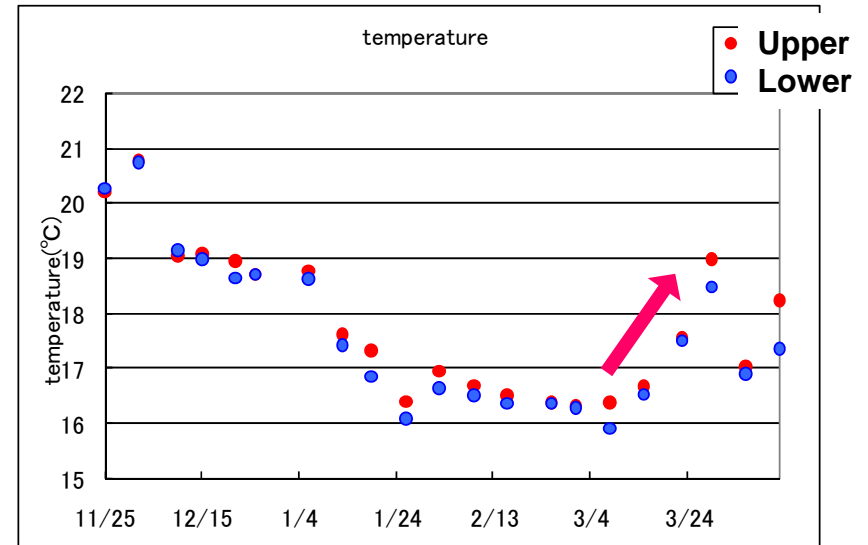
1. High growth potential/no extinction
2. Timing of the bloom

# Examination of biological factors

## Growth rate of *G. catenatum*



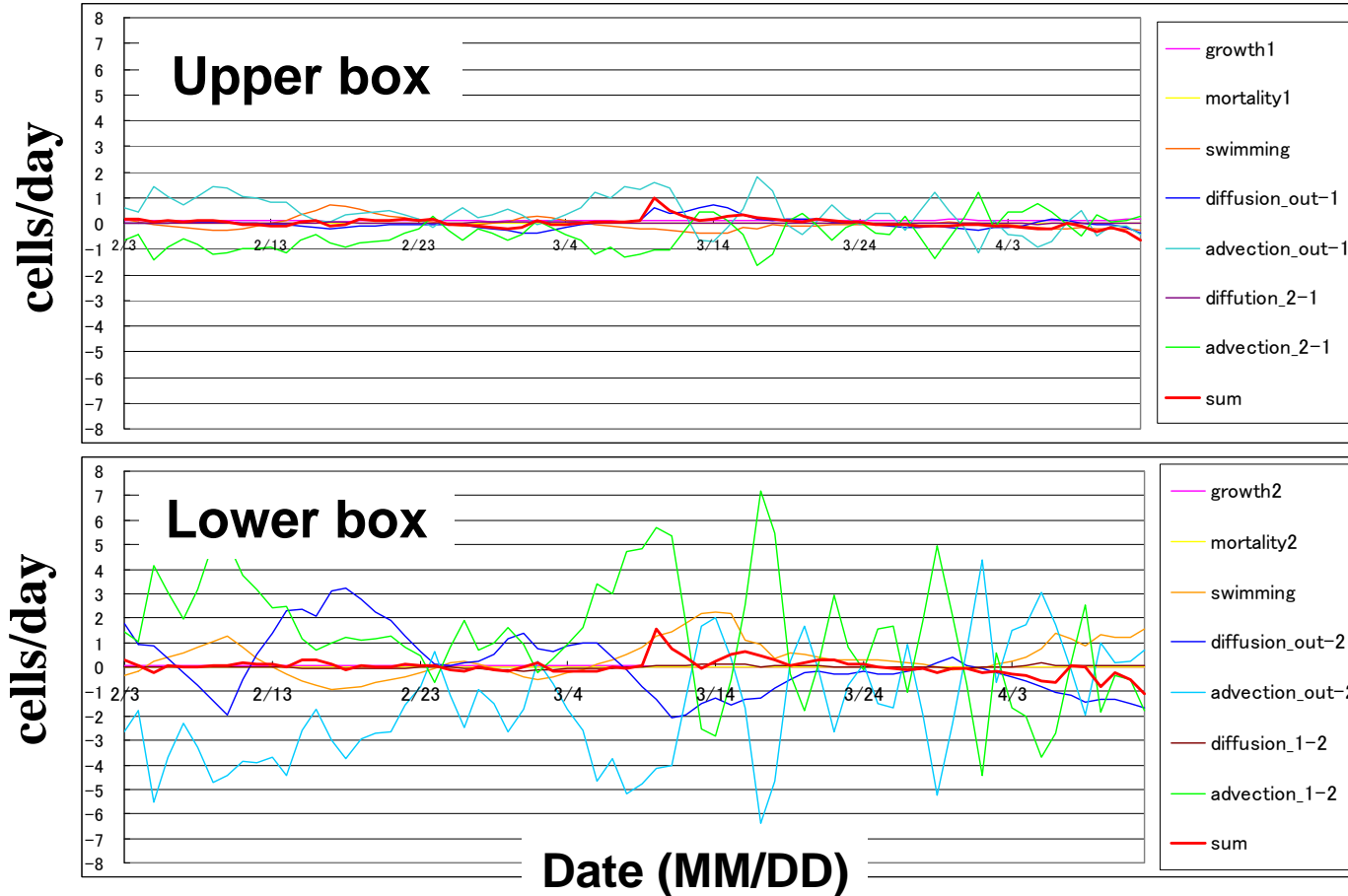
## Temperature



16.5°C → 19.0°C

Temperature is possible

# Examination of biological/physical factors



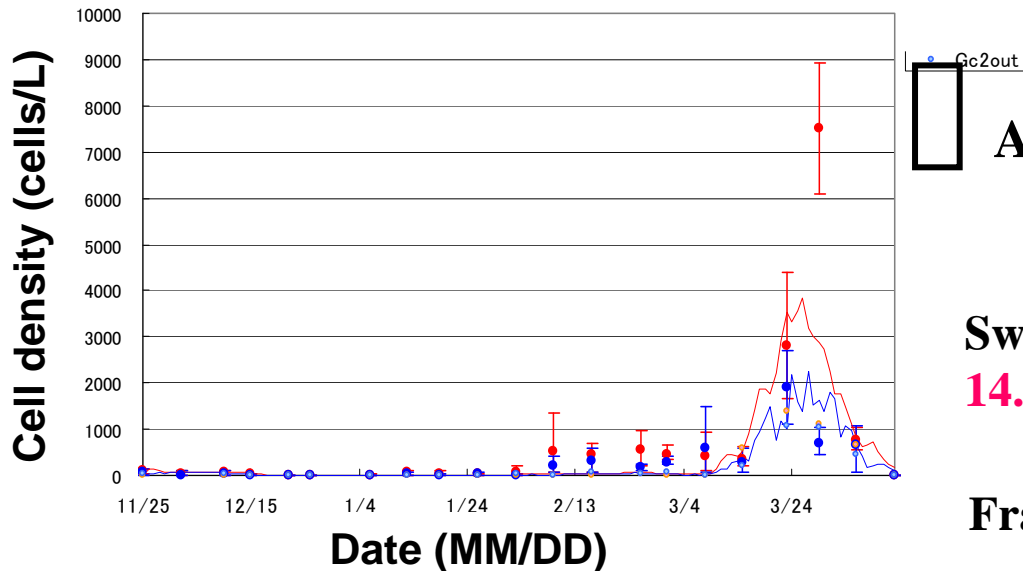
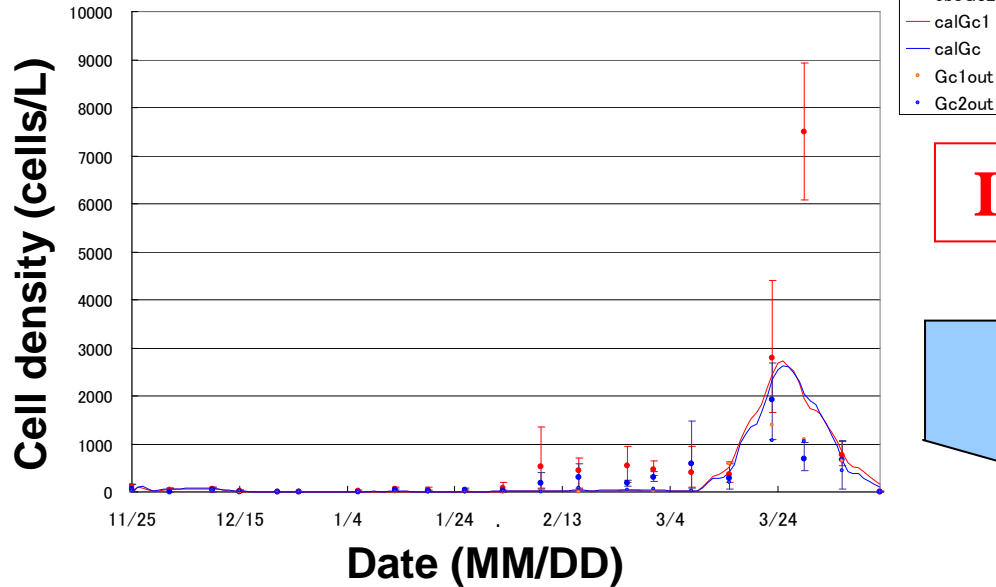
**Changing rate ( $\text{day}^{-1}$ ) = flow (cells/day) / cell density (cells/ $\text{m}^3$ ) / box volume ( $\text{m}^3$ )**

- 1. Physical factors (advection and diffusion) are deterministic,**
- 2. Motility (swimming) is the second effective.**



# Comparison of with/without motility

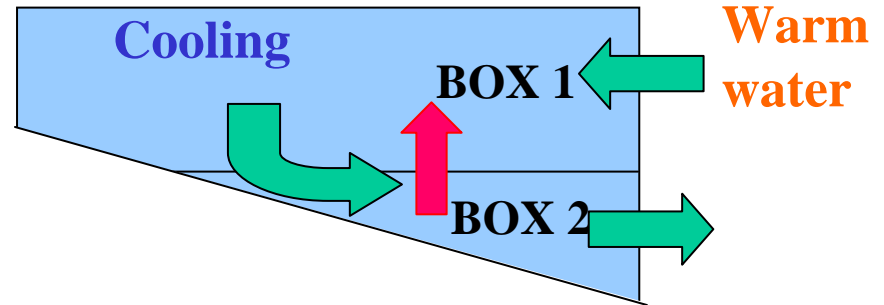
## Cell density of *G. catenatum*



## Flow pattern in winter

### Inverse estuarine circulation

Abo and Miyamura (2005)



Avg adv velocity ca.  $10 \text{ m day}^{-1}$

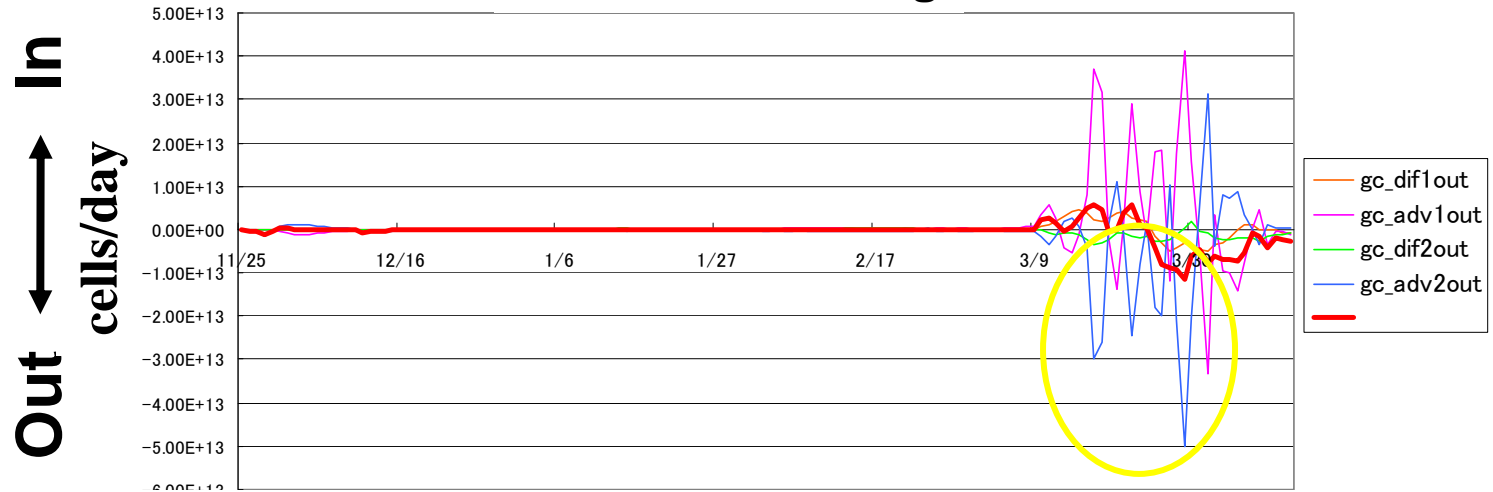
^

Swimming speed of *G. catenatum*  
 $14.88 \text{ m day}^{-1}$  (Anderson and Stolzenbach, 1985)

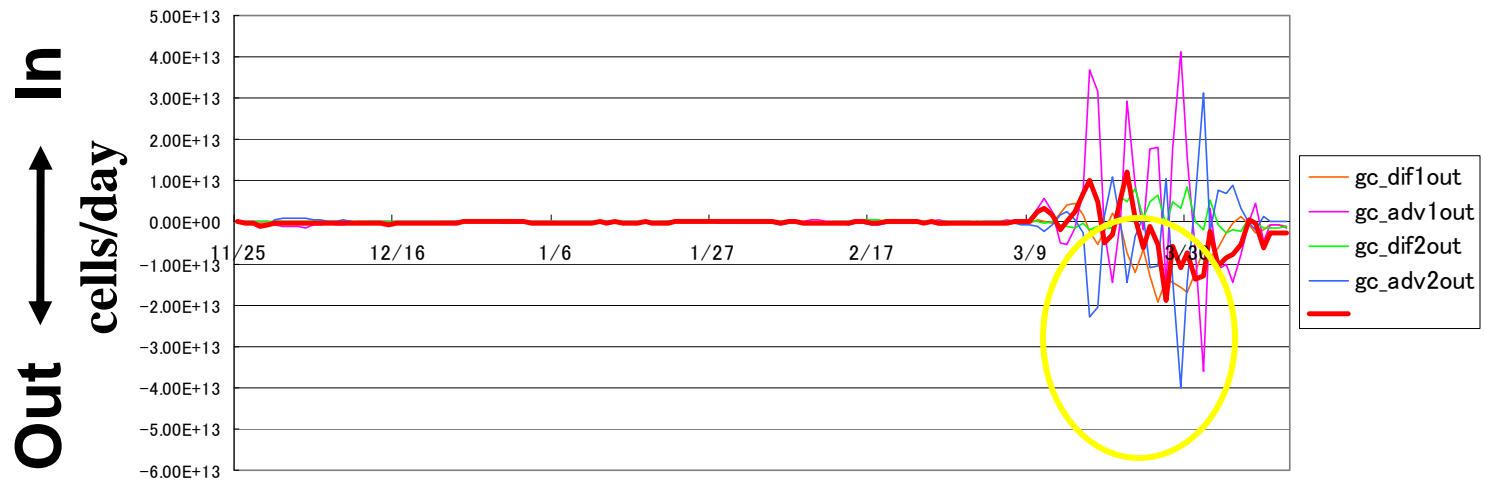
Fraga et al. (1988), Fermin et al. (1996)  
 Ria de Vigo, Spain

# Examination of motility

## Without swimming



## With swimming



**Upward swimming behavior of *Gc* plays an important role to decrease the loss of cells from the lower box to out.**

# Conclusions

- 1. Temperature is a possible factor to accelerate a growth rate at the time of the bloom.**
- 2. Physical processes are the most effective to determine the bloom formation/dissipation of *G. catenatum* in Inokushi Bay.**
- 3. Swimming behavior is likely to be important for *G. catenatum* to maintain their cell density during the period of “inverse estuarine circulation”.**

# Acknowledgements

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