

# The Charminglly Simple Model – adding environmental forcing

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Jake Rice & Niels Daan

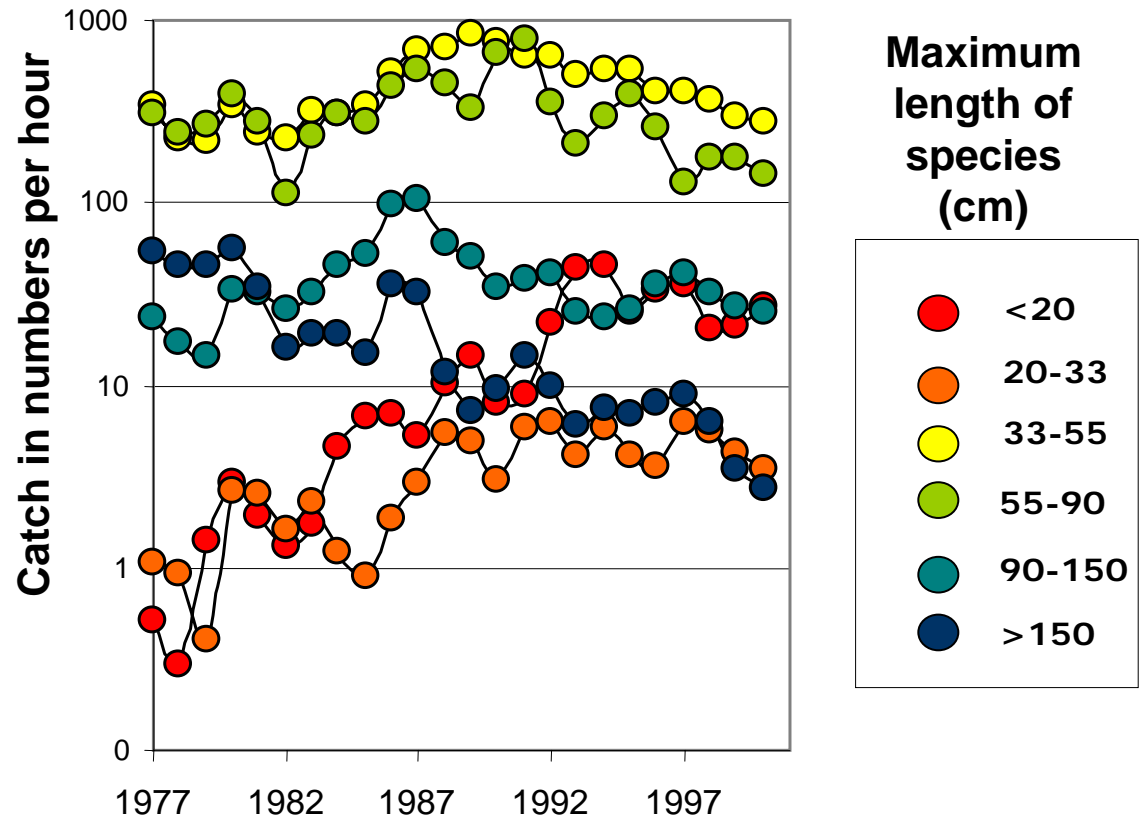
# Fitting GLMs to MSVPA Suitabilities

Diet link of each age of each predator to  
each age of each prey (multiple years)

- SUBSTANTIAL Variance explained by overall SIZE OF Predator covariary
- LITTLE variance explained by
  - Main Effects of Species of Predator, Species of Prey, Year
  - Interactions of the Main Effects
  - Separate Slopes for each predator



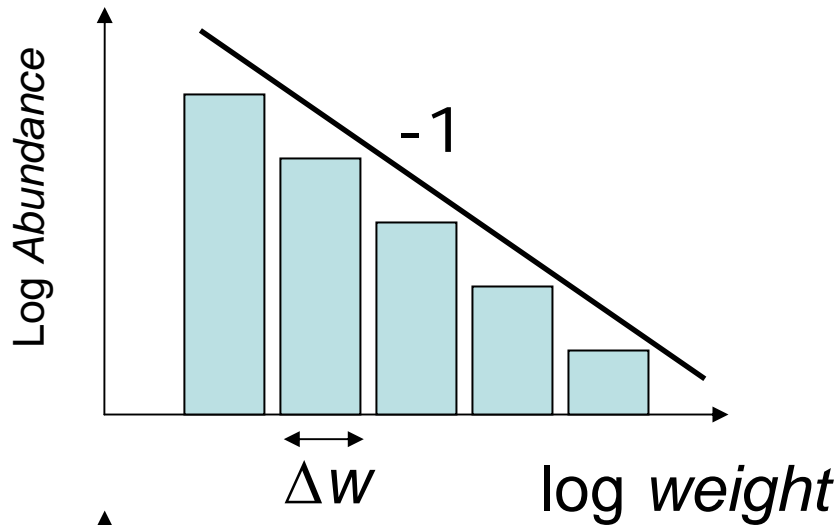
## Changes in the number caught per hour of large and small species



Daan, Gislason, Rice & Pope (2005)

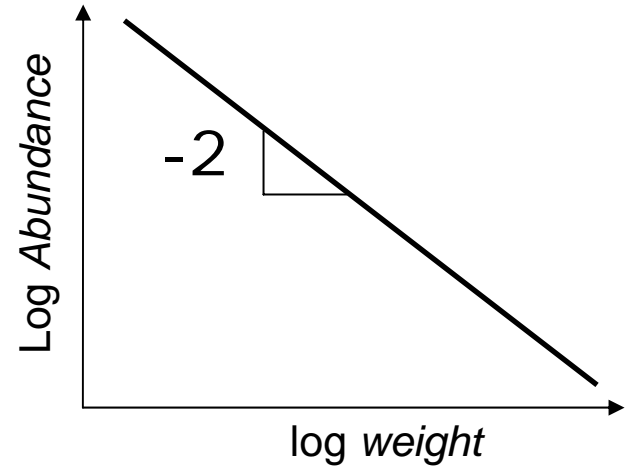
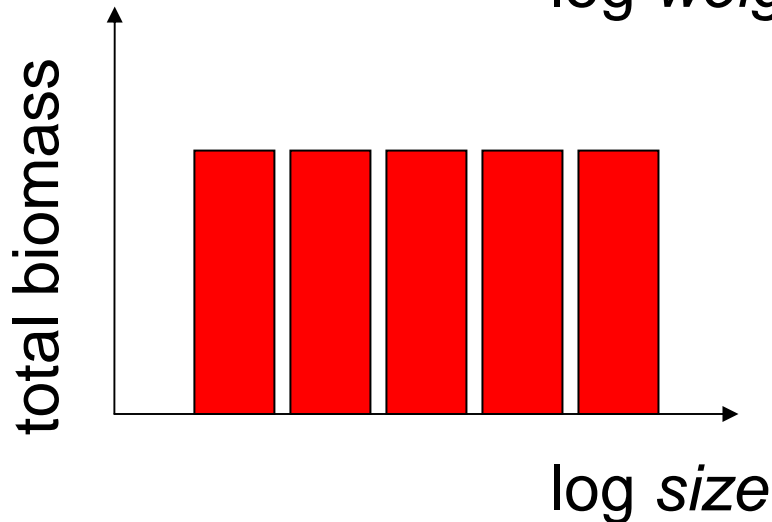
# What is a size spectrum really?

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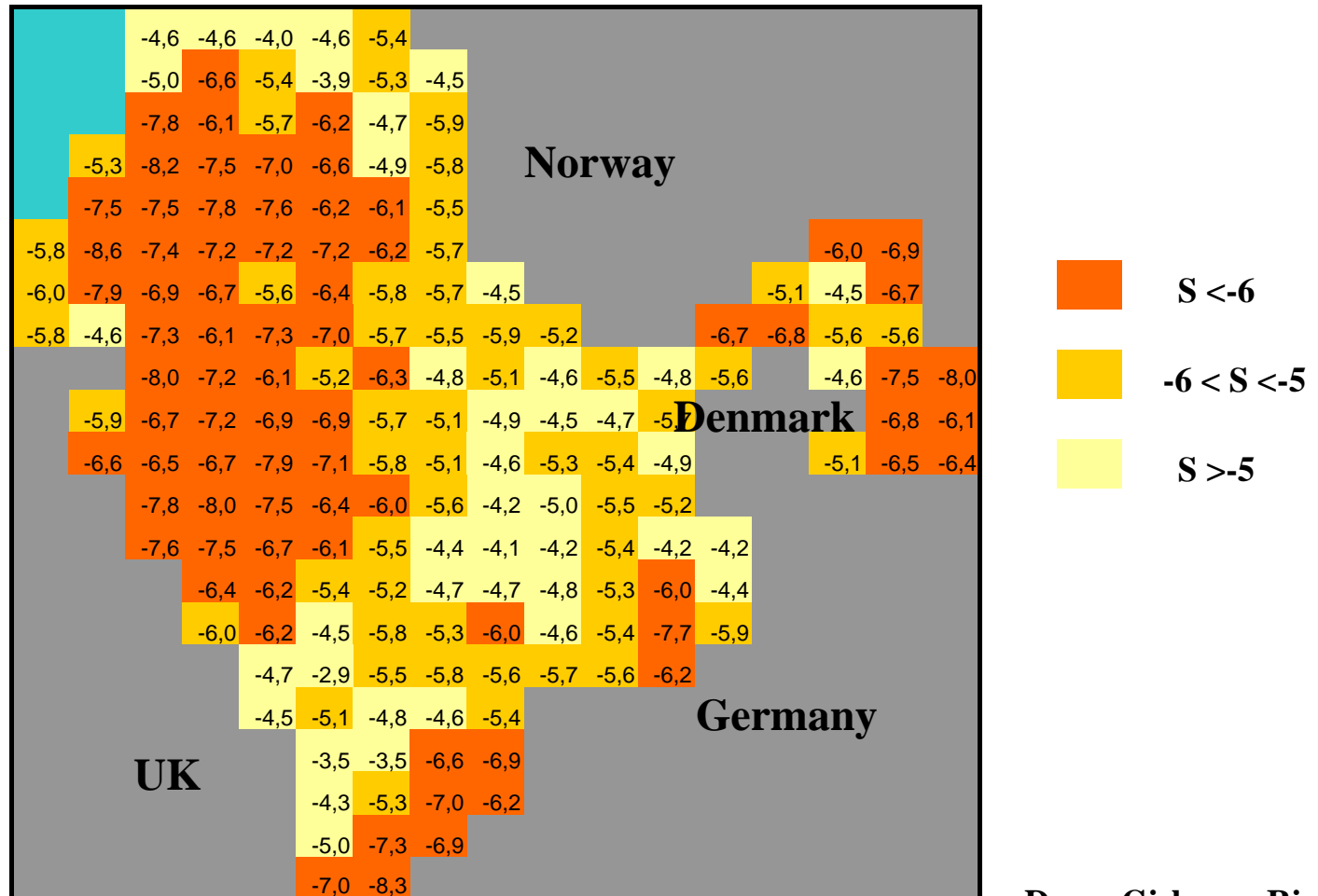


Power law scaling:

$$N = \kappa w^{-\lambda}$$



# Slope of the size spectrum of fish in the North sea, 1980-1999

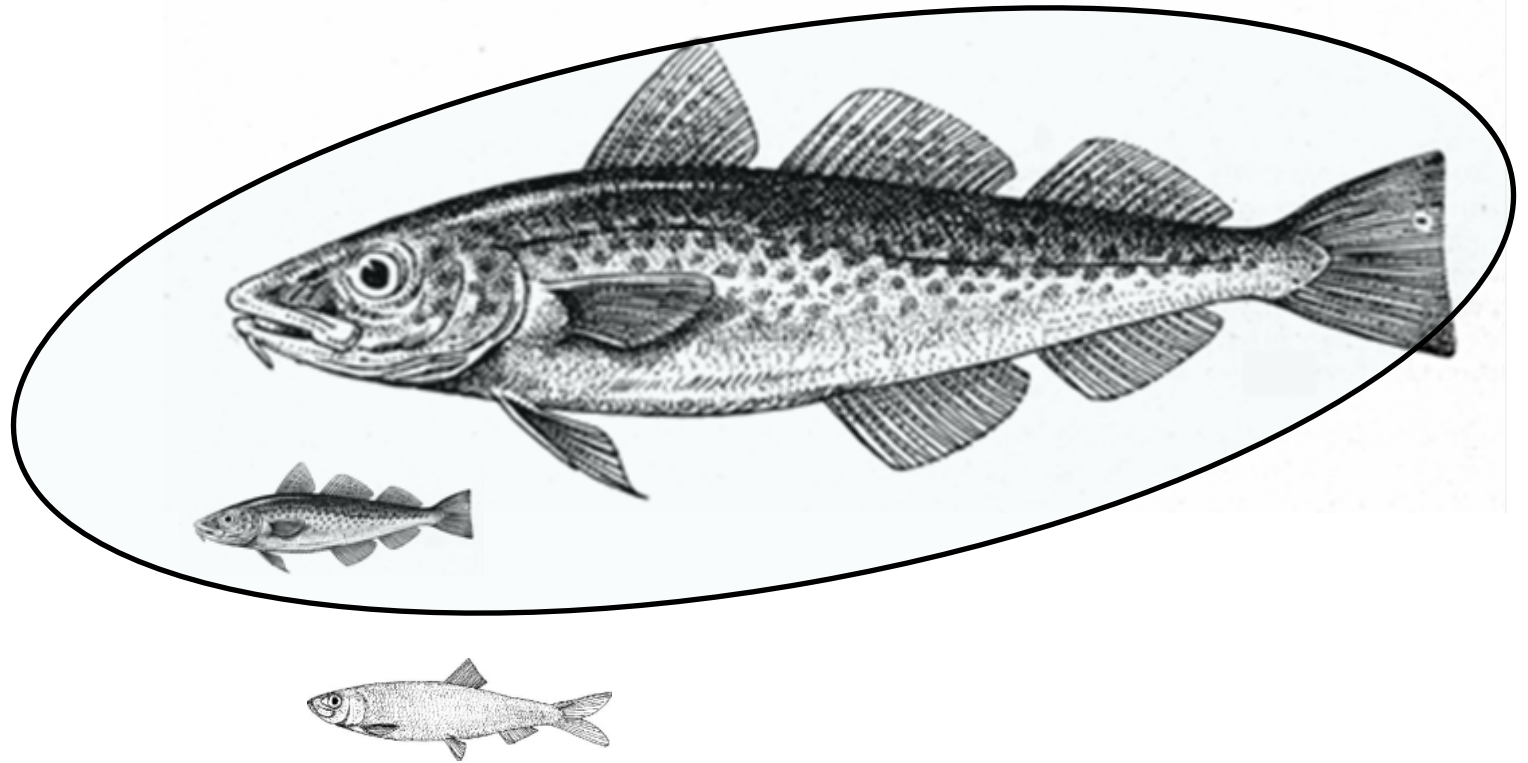


Data from the International Bottomtrawl Survey

Daan, Gislason, Rice & Pope (2005)

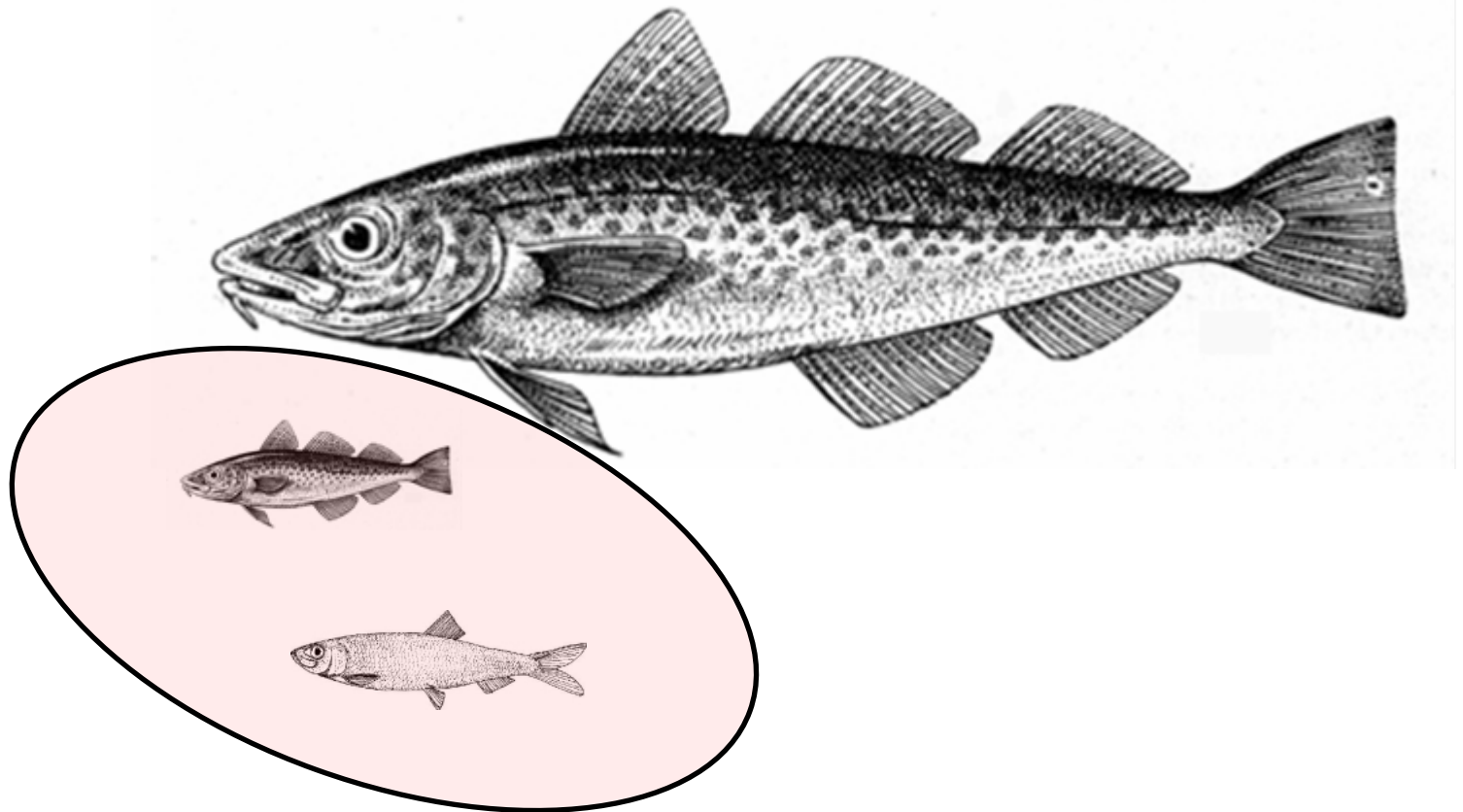
**Which two fish are most similar?**

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Which two fish are **ecologically** most similar?

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*Size is more important than species*

# Ingredients...

Beverton & Holt  
- age based single species

Andersen & Ursin  
North Sea model  
- cohort based ecosystem

Size spectrum theory  
Andersen & Beyer (2006)  
Pope et al (2006)  
Hall et al (2006)



Size-based ecosystem model



# Strategy of model

- Modelling FISH COMMUNITY from smallest estimated by surveys to largest
- Based on ALLOMETRIC SCALING RELATIONSHIPS (Charnov etc)
- Assumes trophodynamic relationships closer to size-based than species based
- Does not pretend to model lower trophic levels
- Allocate  $L_{\infty}$  for community members and let allometric functions assign values for each “species” – total of 15 parameters for 12 species

# Key Equations

- VonBertalanffy growth (2 parameters)
    - Jones length-based cohort analysis
  - Size selectivity of fishery (4 parameters)
    - Logistic selectivity (3); \*Scenario dependent mean F
  - Anderson-Ursin Predation Mortality (4 p)
    - Mean & variance of size ratio, power, constant
  - Maturity at proportion of L (1 parameter)
- 
- \*Power S-R function (3 parameters)
  - \*Scaling M/k ratio with size (1 parameter)

# Variables for Scenarios

Scenario	Key	Density Dependence			
		High	Low	V.low	
• M/K ratio	$\tau$	0.8	0.8	0.9	1.
• Stock Recruitment					
– power ssb	$\phi$	0.45	0.25	0.75	0.95
– power Linf	$\phi$	-3.55	-3.90	-3.10	-2.66
• const	$\rho$	18.0	20.3	14.7	12.4

# Constraints

- **F** ~ **mean F** on fully recruited size classes of all species in the North Sea (.7) with 50% selection at 30% of  $L_{\infty}$ .
- **A size spectrum slope** ~ 0.1 **per** cm that was linear over the 20cm to 100cm length range ( $R^2 > 0.95$ ).
- **M2** such that a plot against weight (Wt) was as close as possible to the fitted relationship in MSWG reports
- **A total fish biomass** of about 7 million t with both catch and fish consumption being about 3 million.
- **Catch fish** with  $L_{\infty}$  of 10 and 20cm about half of the total

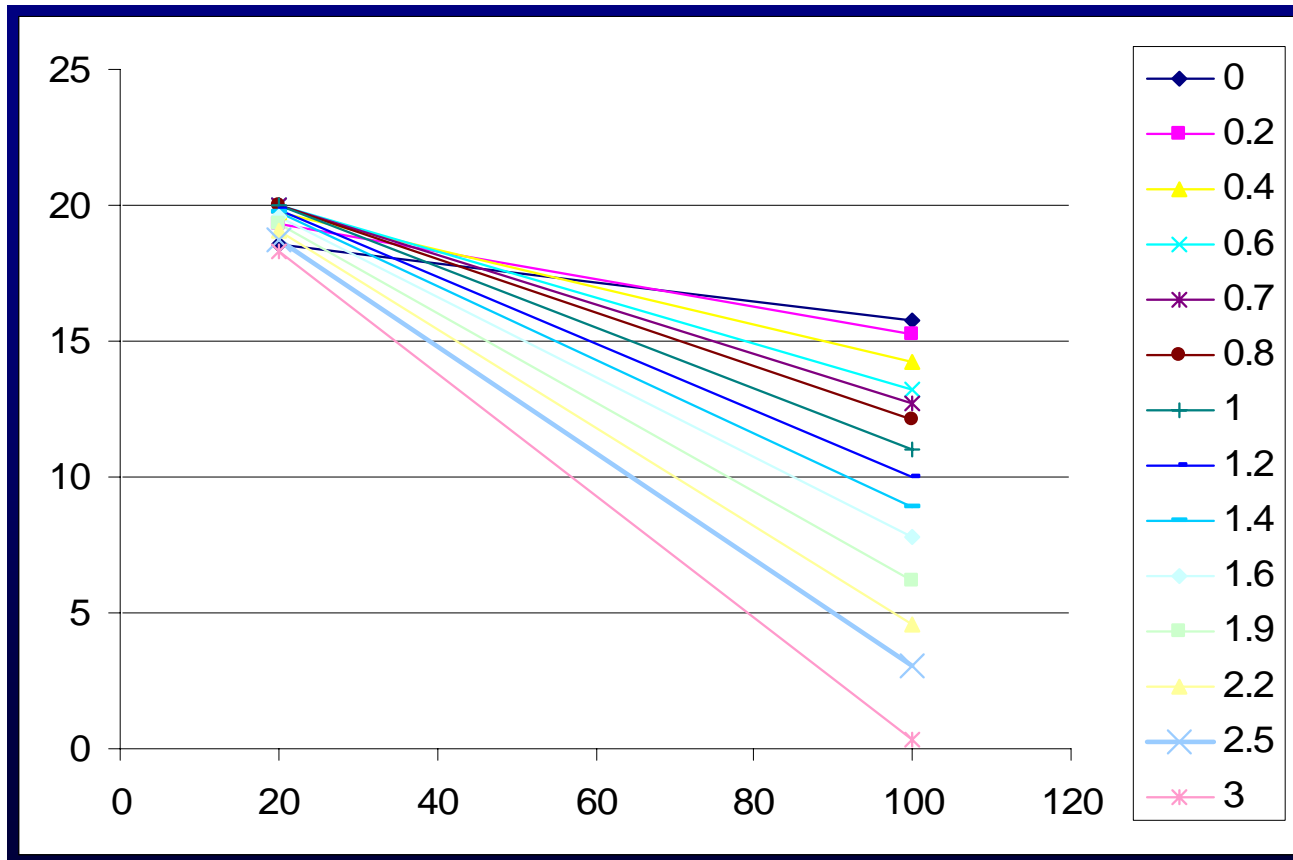
All these have documentation in literature

# Fits to constraints

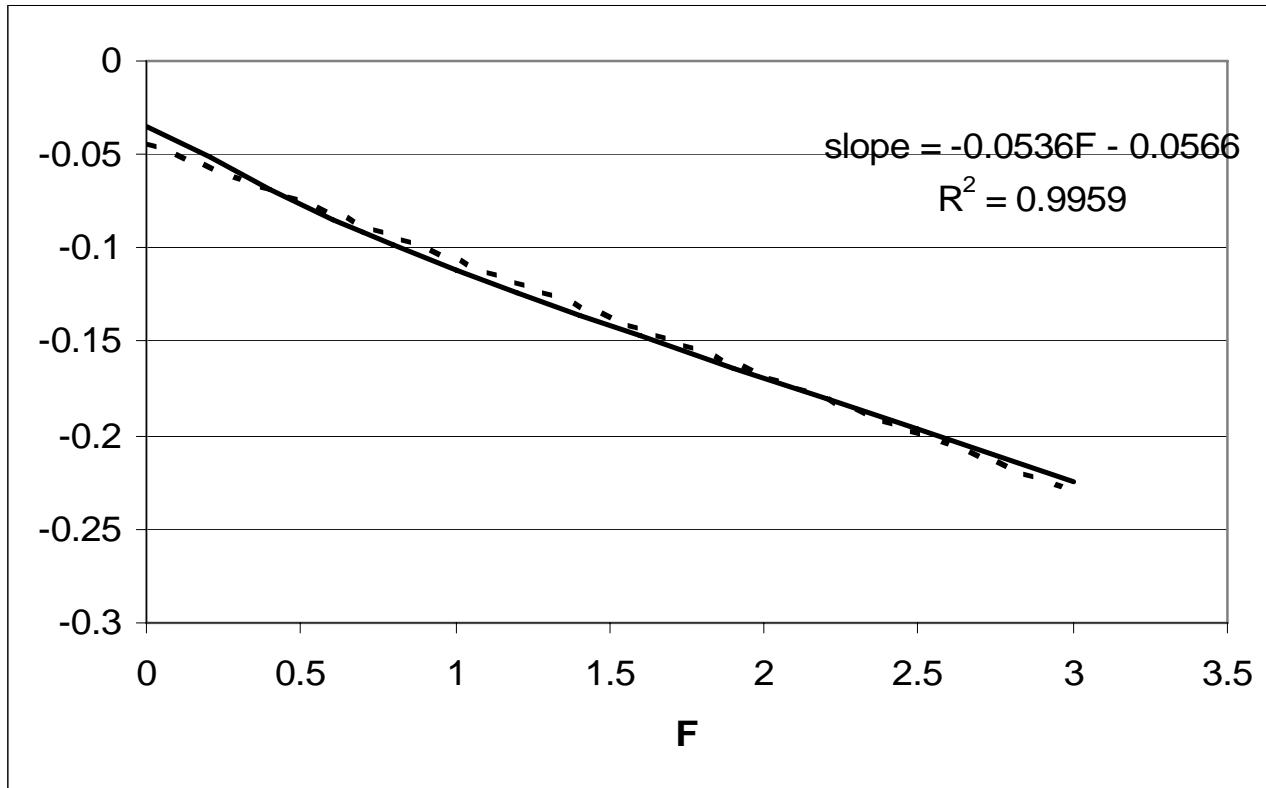
	Target	Key run	2	Scenarios 3	4
• Size Spectra $R^2$					
•	>0.95	0.997	0.997	0.994	0.961
•					
• M2's (year-1) & $\ln(M2)$ on $\ln(Wt)$ regression					
• Max M2	1.50	1.61	1.74	1.37	1.41
•					
• Catch, consumption and biomass (million t)					
• <30cm $L_\infty$ groups	1.50	1.54	1.45	1.74	1.64
• Total catch	3.00	2.97	2.98	3.14	3.13
• Total eaten	3.50	3.50	3.46	3.48	4.00
• <b>Total biomass</b>	<b>7.00</b>	<b>5.04</b>	<b>5.14</b>	<b>5.60</b>	<b>6.07</b>

What types of things can the  
model do?

# Slope as function of F



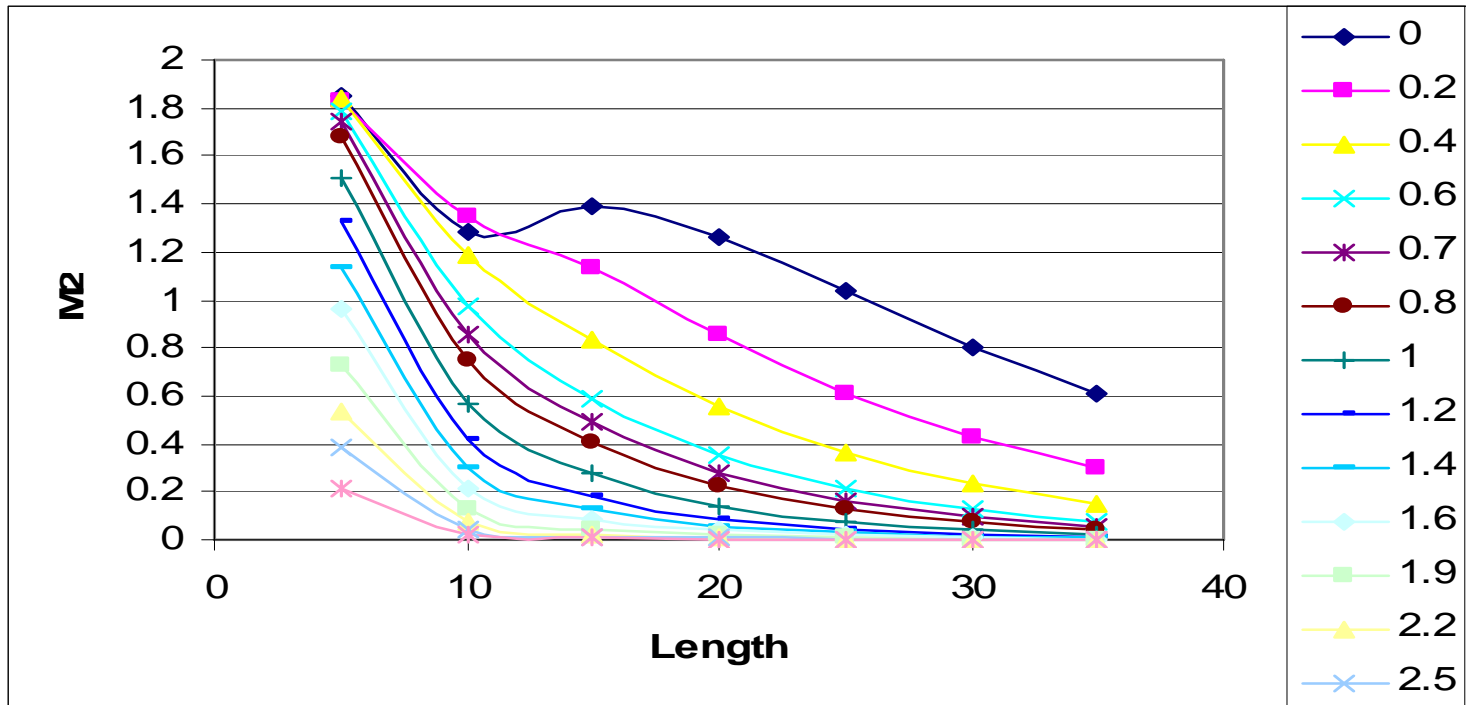
# Regression of slope on F



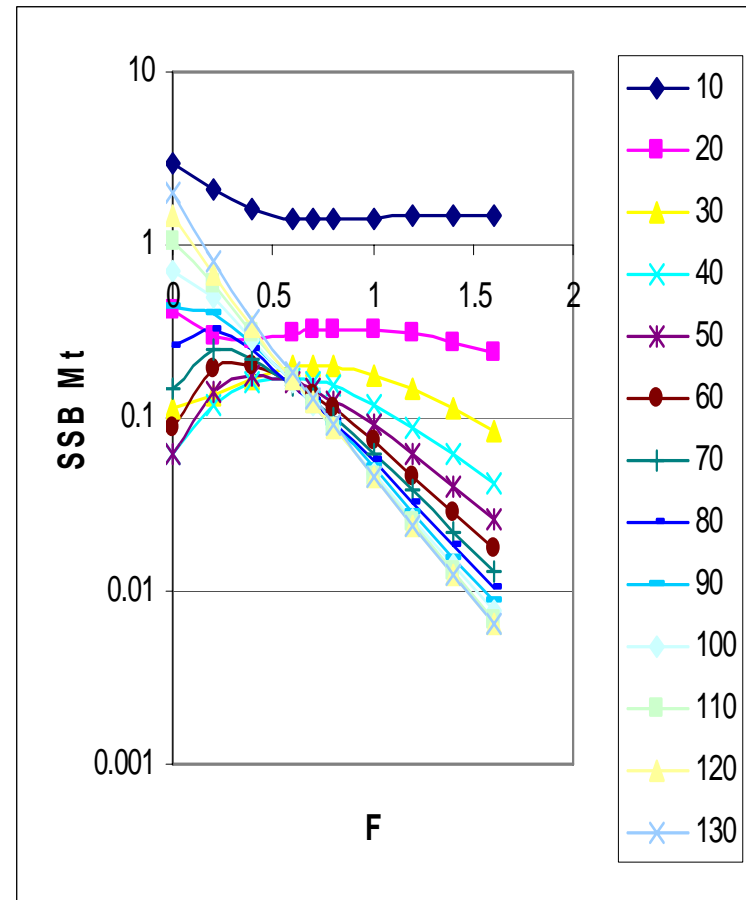
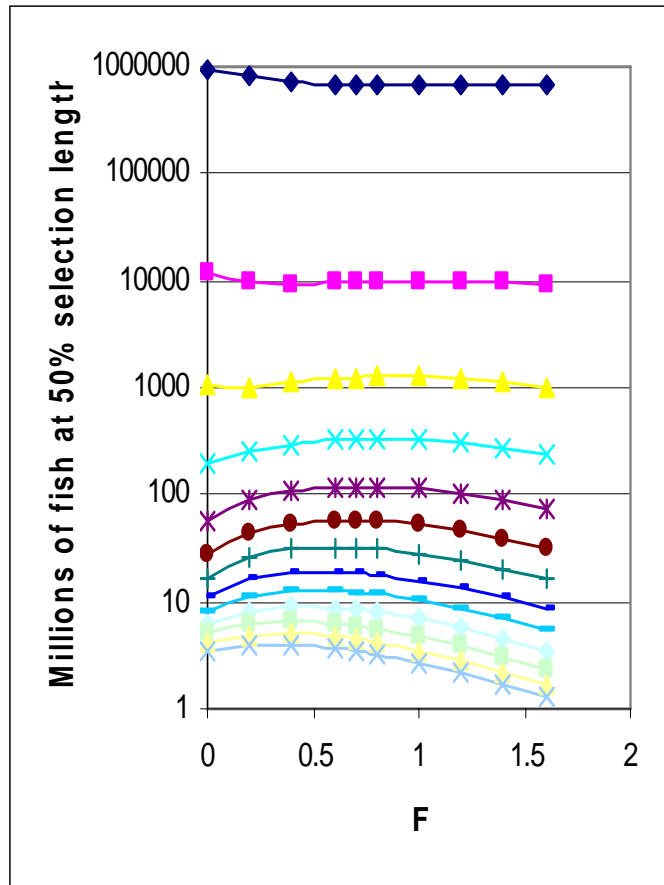




# M2 by size as f(F)



# “Recruitment” and SSB of each $L_\infty$ “species” as f (F)

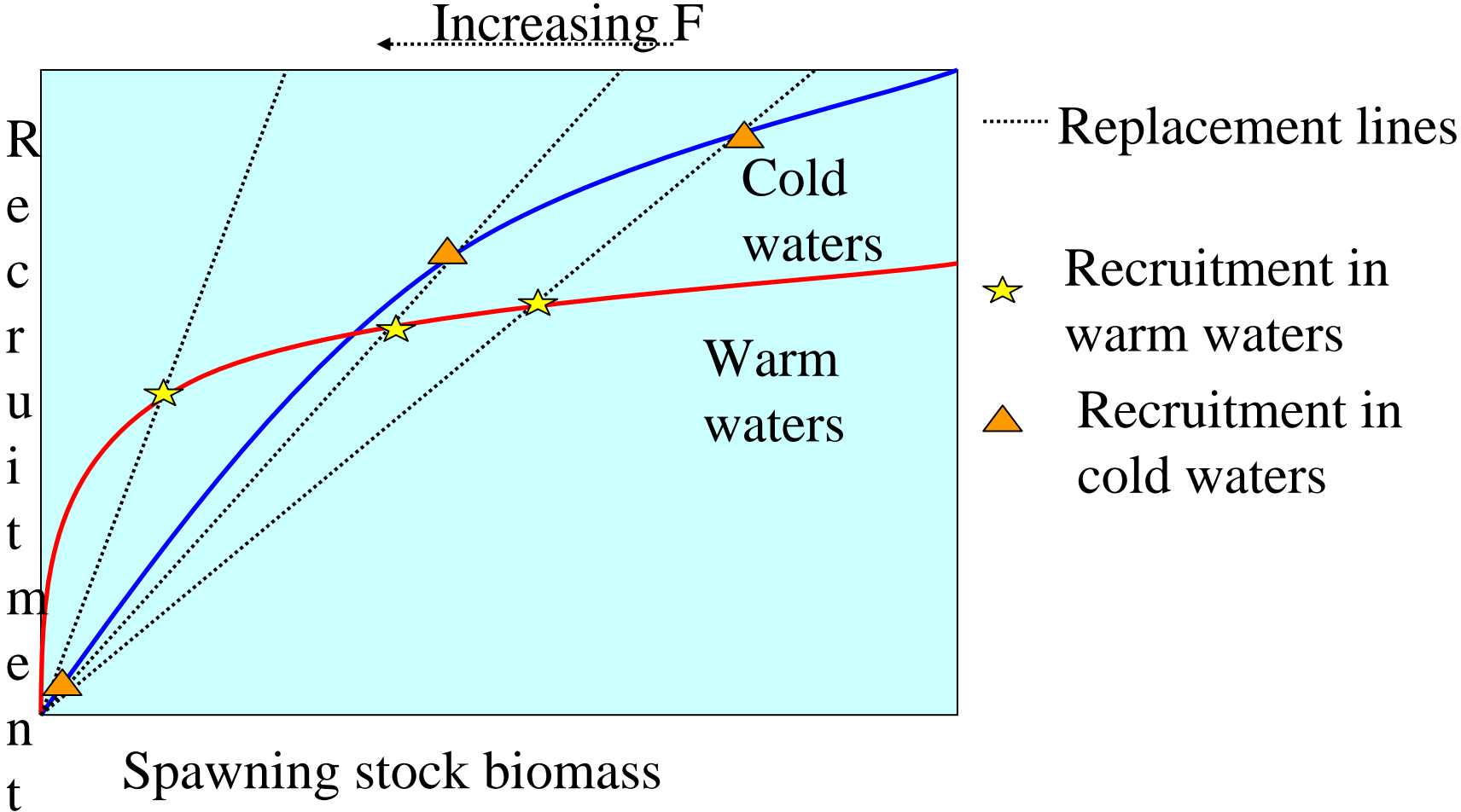


# Charnov and Gillooly 2004: life history parameters scale with temperature and size

- Natural Mortality  $M = \lambda_1 \exp(-E/kT) * m_\alpha^{-0.25}$
- Age first Maturity  $\alpha = \lambda_2 \exp(E/kT) * m_\alpha^{0.25}$
- Spawning Prop.  $c = \lambda_3 \exp(-E/kT) * m_\alpha^{-0.25}$
  
- These were not formulated in terms of the von Bertalanffy parameters the CSM used.
- BUT WE HAVE A CUNNING PLAN

Putting in the Environment

# A linear stock-recruitment relationship makes the community more vulnerable to fishing



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# From Beverton invariant M/K we infer

- von Bert.  $K = \lambda_4 \exp(-E/kT) * m_\alpha^{-0.25}$
- Using  $L_\alpha = L_\infty^{0.93}$
- Thus  $K = \lambda_4 \exp(-E/kT) * L_\infty^{-0.70}$
- Very like the CSM's form
- $K = 4.5 * L_\infty^{-0.67}$
- But with a temperature term  $\exp(-E/kT)$



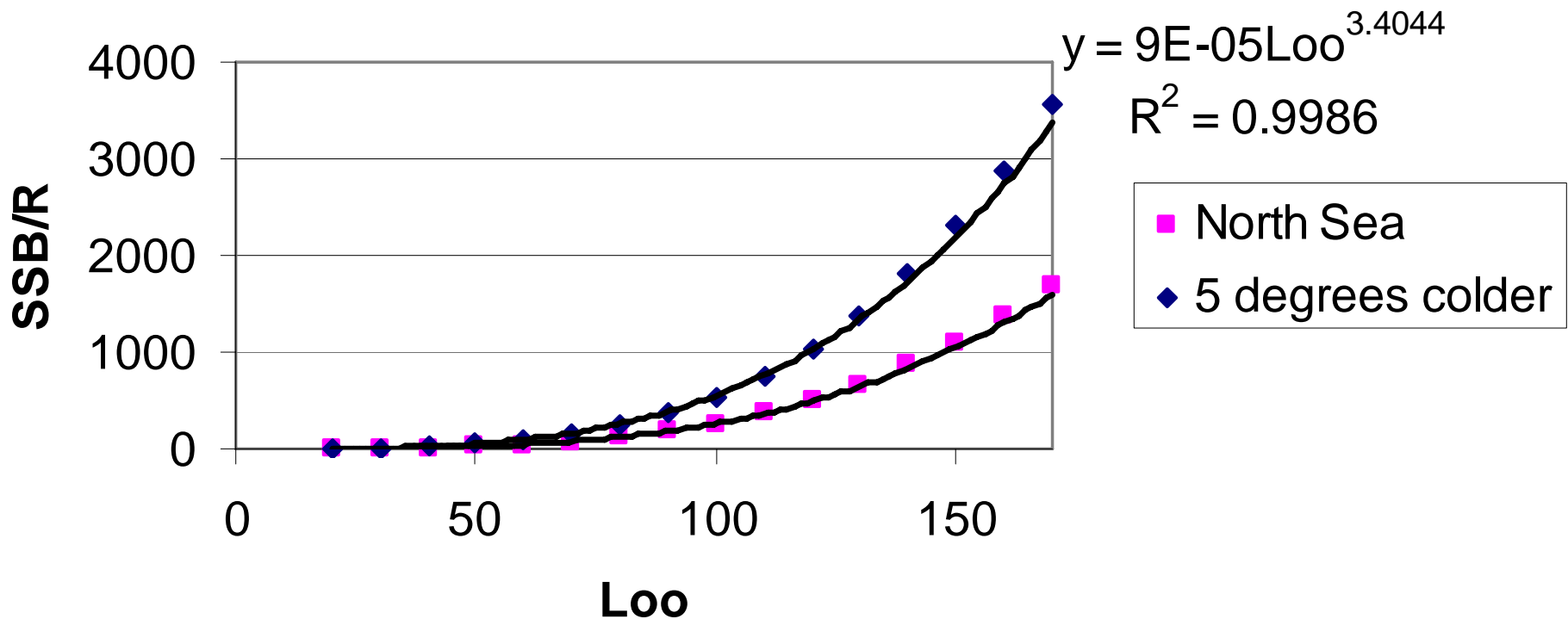
# We can augment the CSM

Use Life History parameters by temperature  
to Calculate for different ecosystems

- SSB/Recruit
- Replacement Lines
- Intersect with Recruitment/ SSB relationship
- Resulting species SSB
- Resulting species total Biomass

# Temperature change maintains relative SSB/R by $L_{\infty}$

## SSB/Recruit by $L_{\infty}$



# Total Biomass: With $\varphi$ close to 1.0 the system is easy to flip.

